

Appendix

Design steps of phase lag network

Step 1: Draw the magnitude and phase for $G(s)$ for the uncompensated system.

Step 2: From Bode plot determine the phase margin of the uncompensated system.

Step 3: If ϕ_s = specified phase margin

ε = margin of safety

$$\phi = \phi_s + \varepsilon$$

Step 4: Determine the frequency corresponding to the required phase margin from the phase curve this frequency is new gain crossover frequency w_m .

Step 5: The magnitude curve is brought down to $0dB$ at the new gain crossover frequency when the phase margin is satisfied, the phase lag network must provide the amount of attenuation equal to the value of magnitude at w'_m

$$|G(jw')| = -20 \log \alpha \quad \alpha > 1$$

$$\alpha = 10^{-|G(jw')| / 20}$$

Step 6: Calculate T from

$$\frac{1}{\alpha T} = \frac{w'_m}{10}$$

Step 7: Draw Bode plot for compensated system and check the phase margin if met or not. If not ad just the value of α and T .