## **DEDICATION**

... To My parents

To My brothers, Sisters, and

... Lovely Friends

#### **ACKNOWLEDGMENT**

Firstly I specify my great thanks to my God for his benefits, facilities, and properties which cover me, then I want to thank deeply Dr.

Mohamed Hassan Mohamed Khabir for his great help in all steps of .this research in spite of his great responsibility

I wish to thank Sudan University of Science and Technology,

.Faculty of Science for the M.Sc chance

Lastly my thanks are due to everyone who; asked, encouraged, and .gave me any help

### **ABSTRACT**

We present in this thesis the cubic B-spline collocation method and its applications to the differential equations. First we have given the derivation of the B-spline method in general. Second, uniform convergence of the method has been discussed. We have applied the method for solving some problems in ordinary and partial differential equations and the numerical results have been compared with the exact solutions.

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تناول نا في هذا البحث طرد قة - ب - اللسينية متحدة الموضعية التكعيبية وتطبي قها على المعادلات التفاضلية. اولا اعطينا الاشت قاق لطرد قة - ب - اللسينية متحدة الموضعية بصورة عامة . ثانيا تمت منا قشة التقارب المنتظم للطرد قة . لا قد قمنا بتطبيق الطرد قة لحل بعض المسائل في المعادلات التفاضلية العاددة والجزئية و قد تمت م قارنة النتائج العددية مع الحلول المضبوطة.

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