

**Sudan University of Science &  
Technology**

**College of Higher Graduation**

**A Study of Some Problems in  
Advanced**

**Complex Variable Theory**

**دراسة بعض المسائل في نظرية المتغير المركب المتقدمة**

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