# **Dedication**

To my family

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### **Abstract**

The semigoroupoid  $C^*$ -algebra is shown to be isomorphic to the algebras usually attached to the corresponding combinatorial object, namely the Cuntz- Krieger algebras and the higher-rank graph  $C^*$ -algebras, respectively. In the case of a higher-rank graph, it follows that the dimension function is superfluous for defining the corresponding  $C^*$ -algebra. We study a tracial notion of Z- absorption for simple, unital  $C^*$ -algebras. We also show that weak cancellation implies the properties for extremally rich  $C^*$ -algebras and that the class of extremally rich  $C^*$ -algebras with weak cancellation is closed under extensions. Moreover, we consider analogous properties which replace the group  $K_1(A)$  with the extremal K-set  $K_e(A)$  as well as two versions of  $K_0$ -surjectivity. We study that von Neumann algebras and separable nuclear  $C^*$ -algebras are stable for the Banach-Mazur cb- distance. A technical step is to show for the unital almost completely isometric maps between  $C^*$ -algebras are almost multiplicative and almost self adjoint.

#### الخلاصة

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