

Dedication

To Our
Fathers,
Mothers,
And
Brothers.

Acknowledgments

First of all , we would like to thank to Allah. The most beneficent , the most merciful , for all his guidance and given while we were preparing , doing and finishing this thesis.

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Abstract

We give a full characterizations of the effect of shift operators , their partial isometries and concrete generalizations we construct the interpolation theorem by which we investigate the Pick-Nevanlinna and Lowner types.

We also show the factorization of Toeplitz and outer operators. The methods of concrete spectral analysis are now shown.

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