## **On Essentially Commuting Toeplitz Operators**

By

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# **Dedication**

To my father, mother, sisters, and brothers.

## Acknowledgement

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### **Abstract**

We present the characterization of subalgebras and Douglas subalgebras. We show the existence of one point maximal antisymmetric sets for H+C and subalgebras of L containing H. we completely characterize compact commutator of two Toeplitz operators on the Hardy space of the unit ball.

#### الخلاصة

تم تشخيص الجبر الجزئي والجبر الجزئي لدو قلاس . ل قد أوضحنا وجود فئات الذ قطة الواحدة غير المتماثلة الأعظمية للفضاء H+C والجبر الجزئي L الذي يحتوي H . وبصورة تامة تم تشخيص مبدل التراص لمؤثر التبولتز على فضاء هاردي على كرة الواحدة .

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