قال الله تعالى:

#### بسم الله الرحمن الرحيم

في خِلْقَ السَّمواتِ والأرضِ واختلافِ اللَّيلِ والنَّهارِ لآياتٍ لأولي الألباب الَّذين يَذْ كُرونَ الله قياماً وقعوداً وعلى جُنوبهم ويتفكَرونَ في خلْق السَّمواتِ والأرضِ ربَّنا ما خلَقْت هذا باطلاًسبحانَك فَقِنَا عذابَ النار}

صدق الله العظيم

سورة آل عمران الآية (190-191)

### **DEDICATION**

#### To my beloved,

parents "Mohamed Elfatih and Fawzia Nadeem", wife and son "Safa and Ahmed", and brothers "Walla and Wail", whom always stand behind me, and gave me ability and strength to proceed on this work. Their love and affection help me stand where I am. To all of those encouraged me to carry out this work

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#### **ABSTRACT**

This thesis presents derivation of a trajectory tracking and posture stabilizing controller for a differentially-driven Wheeled Mobile Robot (WMR). The robot vehicle is a sturdy platform actuated by Direct Current (DC) motors capable of steering the WMR in different trajectories. For trajectory tracking, an essential capability for autonomous operation, a reliable and robust controller is needed. In addition, as the WMR-vehicle is unstable while moving, the controller is required to stabilize it during trajectory tracking process. The robot vehicle is modeled with three Degrees Of Freedom (3DOF) rigid body equations and an efficient control algorithm, called Lypaunov function direct method, is used to tackle the challenges posed by nonlinearities of the model. The main contribution of this work is analysis of 3DOF physical model and a consolidated stable control law for tracking and posture stabilizing of the mobile robot. Simulation results show the effectiveness of the controller. In addition, the proposed trajectory tracking controller has been benchmarked with the well-known Kanayama's controller. Further, several motion tasks are performed in order to examine the new controller motion capabilities, and the ability of carrying out motion with different trajectories shapes.

#### مستخلص

تقدم هذه الاطروحة نموذج لتصميم وحدة التحكم في تتبع المسار و استقرارية الوضع للربوت المتحرك بعجلات. الربوت المتحرك بعجلات يتكون من منصة قوية تدفعها محركات للتيار المباشر و التي لها القدرة علي توجيهه في مختلف المسارات. الحاجة لوحدة تحكم موثوقة و قوية في العمليات المستقلة (الآلية) أمر ضروري و ذلك لأغراض الحركة و تتبع المسار, كما هو الحال في استخدام الربوت ذو العجلات. علاوة علي ذلك, فان المتحكمة تعمل علي استقرارية الوضع لهيكل الربوت نتيجة لعدم الاستقرارية الذي تنشأ اثناء عملية تتبع المسارات المختلفة. تم اشتقاق النموذج الحركي لهيكل الربوت بثلاثة درجات حرية من معادلات الجسم الصلب, و من ثم استخدمت خوارزمية التحكم (دالة ليبونوف المباشرة) لمعالجة التحديات التي تشكلها الاخطية في النموذج الحركي. تساهم هذه الاطروحة بتحليل النموذج الفيزيائي للربوت المحمول مع ثلاثة درجات حرية, بالإضافة الي تصميم وحدة تحكم موحدة لتتبع المسار و استقرار الوضع, والتي طورت في بيئة وحدة التحكم المصممة. اضافة الي ذلك, تمت مقارنة من قبل (كاناياما). علاوة علي ذلك, تم محاكات العديد من المهام الحركية من اجل فحص مقدرة وحدة التحكم المقترحة و معقدة نسبيا.

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# LIST OF ABBREVIATIONS

**ASM** 

Active Set Model

DC Direct Current

DOF Degrees Of Freedom

FBFN Fuzzy Basis Function Network

FL-ASM Fletcher's Active Set Method

MDOF Multi-Degree of Freedom

MPC Model Predictive Control

N-WMR Nonholonomic-Wheeled Mobile Robot

NF-ASM Non-feasible Active Set Model

PD Proportional–Derivative

PI Proportional-Integral

PID Proportional—Integral—Derivative

PWM Pulse Width Modulation

WMR Wheeled Mobile Robot

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