



# **Dedication**

This work is dedicated to my parents who taught me what really life means .....

To my beloved country Sudan .....

To my and friends and colleagues with love and respect.

## **Acknowledgement**

No work could be accomplished without the help of Allah

Hence countless thanks are due to Allah ,and special thanks go later

Dr.Mohamed Hassan Mohamed khabir with who started this work.

My deep thanks also go to my colleagues, my wife, sons and daughters.

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Fats mother and my father.

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## *Abstract*

In this thesis , first of all ,we consider double Laplace Transform method for the solution general Linear second – order partial differential equations

Double Laplace transform is applied to solve the heat ,wave with constant coefficients and a general telegraph and a partial Integrodifferential equations

The scheme is tested through some examples and the result demonstrate reliability and efficiency of the proposed method .

Also we consider wave and heat and convection equations using the Convolution theorem by replacing non-homogeneous terms with double convolution function and by using convolution.

Finally we apply double Laplace transform to solve the new wave, heat equations with non-constant coefficients.

## الخلاصة

في هذا البحث ، بداية ، اعتبرنا طريقة تحويل لابلاس الثنائي لحل المعادلات التفاضلية الجزئية . طبق تحويل لابلاس الثنائي لحل معادلات الحرارة والموجة بمعاملات ثابتة ومعاداة التلغراف العامة والمعاداة التفاضلية – التكاملية . الطريقة طبقت على بعض الامثلة واطهرت النتائج كفاءة وفعالية الطريقة المستخدمة . ايضا استخدمنا نظرية الالتفاف لحل معادلات الحرارة والموجة ومعادلة حركة الهواء الافقية بتحويل الحدود غير المتجانسة باستخدام التفاف الدوال الثنائي والالتفاف الفردي .

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