

بِسِ مِٱللَّهِٱلرَّحْمَزِٱلرَّحِي

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Faculty of Engineering

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Synthesize of Design of

Lateral Autopilot

Thesis Submitted in Partial Fulfillment of the Requirements for the Degree of Bachelor of Science. (BSc Honor)

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الآية قال تعالى:

(... إِنَّمَا يَخْشَى اللهَ مِنْ عِبَادِهِ الْعُلَمَاءُ...)

سورة فاطر/جزء من آية 28

ABSTRACT

Autopilot systems have been until now crucial to flight control for decades and have been making flight easier, safer, and more efficient.

This is a report of a project aimed to Synthesize of Design by modeling and simulating a lateral autopilot for Boeing747-E by going through all design steps starting from longitudinal derivatives ends to evaluation using assumptions of equations of motions, MATLAB and control theories.

The longitudinal motion has two modes: short mode and Long mode (phugoid), results showed a stability problem at the long period (phugoid), solved by fixing a PD controller. Lateral motion has three modes; rolling, spiral, and Dutch roll. The dynamic response was oscillated during Dutch roll mode. The challenge is to make the passengers comfortable that not to sense the oscillation. Thus to enhance the stability a gain (K_r) were added in the feedback loop.

Results were presented as a dynamic response in the time domain and analyzed using root locus to evaluate the addition of the controllers on the longitudinal and lateral stability, the location of the poles and zeros on the plan and their effect on the modes was clear and positives.

التجريد

قد كان نظام الطيار الآلي حاسما في التحكم في الطير ان منذ عقود،وقد جعل الرحلة أسهل و أكثر أمنا ، وبالتالي أصبح نعمة لصناعة الطير ان.

نظام الطيران الآلي يتعامل مع استقرار الطائرة للديناميات الطولية والعرضية , وفي هذا البحث سوف يسلط الضوء علي ديناميات استقرارية الطائرة الجانبية التي لديها مزيد من التحدي لأسباب عديدة. لذا فإن الغرض الأساسي من هذا البحث هو إعادة تصميم و تقييم أداء الطيار الآلي الجانبي علي الاستجابة الديناميكية عن طريق البرامج وتحديد البوينغ E -747 كنموذج للتعامل معها ،و ان قد تم استخدام المشتقات الهوائية و الاستقرارية وجميع المواصفات للبوينغ E -747 التي نحتاجها لوضع النموذج والتحقق من مشتقات استقراره.

كنتيجة لهذا تبين أن الوضع فترة طويلة للطائر ات في الحركة الطولية (phugoid) لديه مشكلة من الاستقر ار وهو في حاجة للسيطرة. أيضا للحركة الجانبية للطائرة التي تعتبر الجزء الرئيسي من المشروع والتي لديها اكثر من طريقة مقارنة مع الحركة الطولية و كذلك أيضا تحديات و مشاكل اللفة الهولندية (Dutch roll)و تأثيره علي الاستقر ار الأفقي.

لحل هذه المشاكل ،كان العمل مع نموذج تحكم ،و هذا يتحقق باستخدام وحدة تحكم(PD)و مربع أداة التحكم للمحاكاة (SIMULINK) ،اللسيطرة الصحيحة عن كثب و مناسبة الاستجابة الديناميكية للطائرة في الحركات الطولية والعرضية.

و هذا يعني أنه يمكن القول بأن النتائج مرضيه،و كذلك العمل مع تقييم الطيار الآلي الجانبي.

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DEDICATION

Our parents: Thank you for your unconditional support with our studies. We are honoured to have you as our parents. Thank you for giving us a chance to prove and improve ourselves through all our walks of life. Please do not ever change. We love you.

Our family: Thank you for believing in us; for allowing us to further our studies. Please do not ever doubt our dedication and love for you.

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List of Symbols

Greek Letters

α	Angle of attack
β	Side-slip angle
δ_{a}	Aileron deflection
$\delta_{ m e}$	Elevator deflection
δ_{T}	Throttle total deflection
λ	Root of modes
Ψ	Heading angle
θ	Pitch angle
φ	Roll angle
ω_n	Natural frequency
ζ	Damping ratio

Small Letters

C_L	Lift coefficient
C_{L_p}	Proportional portion of lift coefficient signal
$C_{L_{\alpha}}$	Lift curve slope
C _D	Drag coefficient
g	Gravitational acceleration
m	Aircraft mass
р	Roll rate

q	Pitch rate
q	Dynamic pressure
r	Yaw rate
u	Velocity of aircraft in the x-body direction
V	Body frame side velocity in the y-body direction
W	Body frame velocity in the z-body direction
х	The state vector
х	The derivative of state vector
У	Output vector

Capital Letters

А	State matrix of a state space representation
В	Input matrix of a state space representation
С	Output matrix of a state space representation
D	Carry through term matrix of a state space representation
I _{xx}	Moment of inertia about the x-body axis
I _{yy}	Moment of inertia about the y-body axis
I _{zz}	Moment of inertia about the z-body axis
I _{yz}	Product of inertia
I _{xz}	Product of inertia
I _{xy}	Product of inertia
W	Aircraft weight

1 Chapter One: Introduction

1.1 Overview

An autopilot is a mechanical, electrical, or hydraulic system used in an aircraft to relieve the human pilot. The original use of an autopilot was to provide pilot relief during cruise modes. Autopilots perform functions more rapidly and with greater precision than the human pilot. In addition to controlling various types of aircraft and spacecraft, autopilots are used to control ships or sea-based vehicles.

An autopilot is unique pilot. It must provide smooth control and avoid sudden and erratic behavior. The intelligence for control must come from sensors such as gyroscopes, accelerometers, altimeters, airspeed indicators, automatic navigators, and various types of radio-controlled data links. The autopilot supplies the necessary scale factors, dynamics (timing), and power to convert the sensor signals into control surface commands. These commands operate the normal aerodynamic controls of the aircraft.

1.2 Aim and Objectives

1.2.1 Aim

- Study of synthesize of design of Boeing747-E aim autopilot.
- Focus on lateral autopilot design and analysis of its performance.
- Propose a controller for the lateral autopilot for Boeing747-E to enhance the dynamic behavior of it.

1.2.2 Objectives

- Propose a suitable method for simulate the lateral autopilot.
- Evaluate the performance.
- Propose and modify lateral autopilot.

1.3 Statement of the Problem

The nonlinearity nature of lateral autopilot is a big challenge for its complex nature and multimode oscillation and more control surfaces are involving in.

Boeing747-E is chosen to make Synthesize of Design and analysis.

1.4 proposed solution

The primary purpose of this research work is to redesign and evaluate the performance of lateral autopilot on the dynamic response by means of software of Boeing747-E.

1.5 Methodology

The methodology will used in the project contain of theoretical, analytical, and simulation methods.

Case study is a fixed wing aircraft. The Synthesize of Design procedures for the controller model will be applied through the process below:

- 1. Aircraft model description
 - a. Basic specification (weight, size, aerodynamic data, and hence the dynamic stability characteristics) of Boeing747-E.
 - b. Linearization and decomposition of the equations
 - c. Check stability derivatives.
 - d. State space modeling of the aircraft.
- 2. controller model
 - a. Calculate aerodynamic forces.
 - b. Calculate the dynamic response under specific condition.
 - c. Use aerodynamic forces and equations of motion to obtain controller model.
 - d. Analysis.
 - e. Simulation
- 3. Calculations supplement in chapter three file.
- 4. Solve the equation of motion for longitudinal stability.
- 5. Check lateral stability.
- 6. Simulation and practical implementation of the controller.
- 7. Evaluate using Root locus.
- 8. Analysis and comparison of the results.

1.6 Thesis Outline

Chapter One: Introduction Chapter Two: Literature Review Chapter Three: Calculation Chapter Four: Results Chapter Five: Discussion Chapter Six: Conclusion Appendices

2 Chapter Two: Literature Review

2.1 History and Background

2.1.1 Introduction

"An autopilot is a mechanical, electrical, or hydraulic system used in an aircraft to relieve the human pilot. The original use of an autopilot was to provide pilot relief during cruise modes. Autopilots perform functions more rapidly and with greater precision than the human pilot. In addition to controlling various types of aircraft and spacecraft, autopilots are used to control ships or sea-based vehicles". [1]

"An autopilot is unique pilot. It must provide smooth control and avoid sudden and erratic behavior. The intelligence for control must come from sensors such as gyroscopes, accelerometers, altimeters, airspeed indicators, automatic navigators, and various types of radio-controlled data links. The autopilot supplies the necessary scale factors, dynamics (timing), and power to convert the sensor signals into control surface commands. These commands operate the normal aerodynamic controls of the aircraft".[1]

2.1.2 Replacement of Human Pilot

"In the aircraft control systems, human pilots play a very important role as they have certain advantages. Human pilots are highly adaptable to unplanned situations, means they can react according to the desired conditions. Also they have broad-based intelligence and can communicate well with other humans". [1]

"But still autopilots have advantages over the human pilot which forced it to replace human pilot. These advantages are described below.

- 1) Autopilots have high reaction speed as comparison to human pilot.
- 2) They can communicate well with computers, which is difficult for human.
- 3) They can execute multiple events and tasks at the same time.
- 4) They also eliminate risk to on-board pilot.

Autopilot relieves human pilot from fatigue".[1]

2.1.3 Flight Control System

"A flight control system is either a primary or secondary system. Primary flight controls provide longitudinal (pitch), directional (yaw), and lateral (roll) control of the aircraft. Secondary flight controls provide additional lift during takeoff and landing, and decrease aircraft speed during flight, as well as assisting primary flight controls in the movement of the aircraft about its axis. Some manufacturers call secondary flight controls auxiliary flight controls, All systems consist of the flight control surfaces, the respective cockpit controls, connecting linkage, and necessary operating mechanisms. Basically there are three type of flight control systems as discussed below". [1]

2.1.3.1 Mechanical

"Mechanical flight control systems are the most basic designs. They are basically unboosted flight control systems. They were used in early aircraft and currently in small aero planes where the aerodynamic forces are not excessive. The flight control surfaces (ailerons, elevators, and rudder) are moved manually through a series of push-pull rods, cables, bell cranks, sectors, and idlers. Since an increase in control surface area in bigger and faster aircraft leads to a large increase in the forces needed to move them, complicated mechanical arrangements are used to extract maximum mechanical advantage in order to make the forces required bearable to the pilots. This arrangement is found on bigger or higher performance propeller aircraft.

Some mechanical flight control systems use servo tabs that provide aerodynamic assistance to reduce complexity. Servo tabs are small surfaces hinged to the control surfaces. The mechanisms move these tabs, aerodynamic forces in turn move the control surfaces reducing the amount of mechanical forces needed.

This arrangement was used in early piston-engined transport aircraft and early jet transports".[1]

The primary flight control system is illustrated in Figure (2-1).



Figure (2-1): primary control system

2.1.3.2 Hydro mechanical

"They are power boosted flight control systems. The complexity and weight of a mechanical flight control systems increases considerably with size and performance of the airplane. Hydraulic power overcomes these limitations. With hydraulic flight control systems aircraft size and performance are limited by economics rather than a pilot's strength. In the power-boosted system, a hydraulic actuating cylinder is built into the control linkage to assist the pilot in moving the control surface. A hydraulic flight control systems has 2 parts:

- 1) Mechanical circuit
- 2) Hydraulic circuit

The mechanical circuit links the cockpit controls with the hydraulic circuits.

Like the mechanical flight control systems, it is made of rods, cables, pulleys, and sometimes chains. The hydraulic circuit has hydraulic pumps, pipes, valves and actuators. The actuators are powered by the hydraulic pressure generated by the pumps in the hydraulic circuit. The actuators convert hydraulic pressure into control surface movements. The servo valves control the movement of the actuators. The pilot's movement of a control causes the mechanical circuit to open the matching servo valves in the hydraulic circuit. The hydraulic circuit powers the actuators which then move the control surfaces. These Powered flight controls are employed in high performance aircraft, and are generally of two types (i) power assisted and (ii) power operated, which are shown in the Figures 2 and 3 respectively. Both systems are similar in basic forms but to overcome the aerodynamic loads forces are required, which decides the choice of either of the above system".[1]



Figure (2-2): Power Assisted Flight Control System



b POWER-OPERATED

Figure (2-3): Power Operated Flight Control System

2.1.3.3 Fly by wire (FBW)

"Fly-by-wire is a means of aircraft control that uses electronic circuits to send inputs from the pilot to the motors that move the various flight controls on the aircraft. There are no direct hydraulic or mechanical linkages between the pilot and the flight controls. The total elimination of all the complex mechanical control runs and linkages-all commands and signals are transmitted electrically along wires, hence the name fly-by-wire and also there is interposition of a computer between the pilot's commands and the control surface actuators which is incorporated with air data sensors which supply height and airspeed information to the computer. The fly-by-wire system is shown in Figure (2-4).



Figure (2-4): Fly-by-wire System

Mechanical and hydraulic flight control systems are heavy and require careful routing of flight control cables through the airplane using systems of pulley and cranks. Both systems often require redundant backup, which further increases weight. Another advantages of FBW system are discussed below:

- Provides high-integrity automatic stabilization of the aircraft to compensate for the loss of natural stability and thus enables a lighter aircraft with a better overall performance.
- 2) Makes the ride much smoother than one controlled by human hands. The capability of FBW systems to maintain constant flight speeds and altitudes over long distances is another way of increasing fuel efficiency. The system acts much like cruise

controls on automobiles: less fuel is needed if throttles are untouched over long distances.

3) More reliable than a mechanical system because of fewer parts to break or malfunction. FBW is also easier to install, which reduces assembly time and costs. FBW maintenance costs are lower because they are easier to maintain and troubleshoot, and need fewer replacement parts.

Electrical wires for a flight control system takes up less space inside fuselages, wings, and tail components. This gives designers several options. Wings and tail components can be designed thinner to help increase speed and make them aerodynamically cleaner, and also to reduce weight. Space once used by mechanical linkages can also be used to increase fuel capacities to give the aircraft greater range or payload".[1]

2.1.4 History

"In the early days of transport aircraft, aircraft required the continuous attention of a pilot in order to fly in a safe manner. This created very high demands on crew attention and high fatigue. The autopilot is designed to perform some of the tasks of the pilot.

The first aircraft autopilot was developed by Sperry Corporation in 1912. The autopilot using gyros to sense the deviation of the aircraft from the desired attitude and servo motors to activate the elevators and ailerons was built under the direction of Dr. E. A. Sperry. The apparatus, called Sperry Aero plane Stabilizer, installed in the Curtis Flying Boat, Won prominence on the 18th June, 1914. Elmer Sperry demonstrated it two years later in 1914, and proved his credibility of the invention, by flying the plane with his hands up .

The autopilot connected a gyroscopic attitude indicator and magnetic compass to hydraulically operated rudder, elevator, and ailerons. It permitted the aircraft to fly straight and level on a compass course without a pilot's attention, thus covering more than 80 percent of the pilot's total workload on a typical flight. This straight-and-level autopilot is still the most common, least expensive and most trusted type of autopilot. It also has the lowest pilot error, because it has the simplest controls.

In the early 1920s, the Standard Oil tanker J.A Moffet became the first ship to use autopilot. The early aircrafts were primarily designed to maintain the attitude and heading of the aircraft. With the advent of the high performance aircrafts, new problems have arisen i.e. unsatisfactory dynamic characteristics. To obtain the more performance, several improvements have been done. Now day's modern autopilots are dominating. Modern autopilots generally divide a flight into take-off, ascent, level, descent, approach, landing, and taxi phases.

Modern autopilots use computer software to control the aircraft. The software reads the aircraft's current position, and controls a flight control system to guide the aircraft. In such a system, besides classic flight controls, many autopilots incorporate thrust control capabilities that can control throttles to optimize the air-speed, and move fuel to different tanks to balance the aircraft in an optimal attitude in the air. Although autopilots handle new or dangerous situations inflexibly, they generally fly an aircraft with a lower fuel-consumption than all but a few of the best pilots".[1]

2.1.5 Techniques Available

"The basic aim of an autopilot is to track the desired goal. Autopilot can be displacement type or pitch type. There are different techniques available to design an autopilot like modelfollowing control, sliding mode control, model predictive control, robust control, lyapunov based control, adaptive control and dynamic inversion control. Every technique has its disadvantages, so to improve the disadvantages new techniques are proposed.

Dynamic Inversion is a design technique which is based on feedback linearization, basically it achieves the effect of gain scheduling. This approach transforms the nonlinear system a linear time invariant form. The transformation is then inverted to obtain a nonlinear control law, but the limitation of this technique is that it cannot be applied to nonminimum phase plants. In this technique, the set of existing dynamics are canceled out and replaced by a designer selected set of desired dynamics. Dynamic inversion is similar to model following control, in that both methodologies invert dynamical equations of the plant and an appropriate co-ordinate transformation is carried out to make the system looklinear so that any known linear controller design can be used.

Lyapunov based control design techniques use the Lyapunov's stability theorem for nonlinear systems and come up with adaptive control solutions that guarantee stability of the error dynamics (i.e. the tracking error remains bounded in a small neighborhood about zero) or sometimes assure asymptotic stability (i.e. the tracking error goes to zero). In sliding mode control , the essential idea is to first lay out a path for the error signal that leads to zero.

Then the control solution is found in such a way that the error follows this path, finally approaching zero. In doing so, however, the usual problems encountered are high magnitudes of control and control chattering. In Predictive control, the error signal is first predicted for some future time (based on a model that may or may not be updated in parallel). The control solution at the current time step is then obtained from an error minimization algorithm that minimizes cost function, which is a weighted average of the error signal. In this study of autopilots, classical methods are used to find the response when the command is given".[1]

2.1.6 Components of Autopilot

"The basic components of the autopilot is shown in the figure (2-5).



Figure (2-5): Basic Components of an Autopilot

Aircraft motion is usually sensed by a gyro, which transmits a signal to a computer (see illustration). The computer commands a control servo to produce aerodynamic forces to remove the sensed motion. The computer may be a complex digital computer, an analog computer (electrical or mechanical), or a simple summing amplifier, depending on the complexity of the autopilot. The control servo can be a hydraulically powered actuator or an electromechanical type of surface actuation. Signals can be added to the computers that supply altitude commands or steering commands. For a simple autopilot, the pitch loop controls the elevators and the roll loop controls the aileron. A directional loop controlling the rudder may be added to provide coordinated turns". [1]

2.1.7 Aircraft Dynamics

2.1.7.1 Equation of motion

Equations of motion are equations that describe the behavior of a system in terms of its motion as a function of time (e.g., the motion of a particle under the influence of a force). Sometimes the term refers to the differential equations that the system satisfies (e.g., Newton's second law or Euler–Lagrange equations).[2,3]

2.1.8 Aircraft dynamic modes

The dynamic stability of an aircraft is how the motion of an aircraft behaves after it has been disturbed from steady non-oscillating flight.[2,3]

2.1.8.1 Longitudinal modes

Oscillating motions can be described by two parameters, the period of time required for one complete oscillation, and the time required to damp to half-amplitude, or the time to double the amplitude for a dynamically unstable motion. The longitudinal motion consists of two distinct oscillations, a long-period oscillation called a phugoid mode and a short-period oscillation referred to as the short-period mode.[2,3]

1) Phugoid (longer period) oscillations

The longer period mode, called the "phugoid mode" is the one in which there is a largeamplitude variation of air-speed, pitch angle, and altitude, but almost no angle-of-attack variation. The phugoid oscillation is really a slow interchange of kinetic energy (velocity) and potential energy (height) about some equilibrium energy level as the aircraft attempts to re-establish the equilibrium level-flight condition from which it had been disturbed. The motion is so slow that the effects of inertia forces and damping forces are very low. Although the damping is very weak, the period is so long that the pilot usually corrects for this motion without being aware that the oscillation even exists. Typically the period is 20–60 seconds.[2]

2) Short period oscillations

With no special name, the shorter period mode is called simply the "short-period mode". The short-period mode is a usually heavily damped oscillation with a period of only a few seconds. The motion is a rapid pitching of the aircraft about the center of gravity. The period is so short that the speed does not have time to change, so the oscillation is essentially an angle-of-attack variation. The time to damp the amplitude to one-half of its value is usually

on the order of 1 second. Ability to quickly self damp when the stick is briefly displaced is one of the many criteria for general aircraft certification.[2]

2.1.8.2 Lateral-directional modes

Lateral-directional" modes involve rolling motions and yawing motions. Motions in one of these axes almost always couples into the other so the modes are generally discussed as the Lateral-Directional modes.

There are three types of possible lateral-directional dynamic motion: roll subsidence mode, Dutch roll mode, and spiral mode. [2,4]

1) Roll subsidence mode

Roll subsidence mode is simply the damping of rolling motion. There is no direct aerodynamic moment created tending to directly restore wings-level, i.e. there is no returning "spring force/moment" proportional to roll angle. However, there is a damping moment (proportional to roll rate) created by the slewing-about of long wings. This prevents large roll rates from building up when roll-control inputs are made or it damps the roll rate (not the angle) to zero when there are no roll-control inputs.

Roll mode can be improved by adding dihedral effects to the aircraft design, such as high wings, dihedral angles or sweep angles. [2]

2) Spiral mode

If a spirally unstable aircraft, through the action of a gust or other disturbance, gets a small initial roll angle to the right, for example, a gentle sideslip to the right is produced. The sideslip causes a yawing moment to the right. If the dihedral stability is low, and yaw damping is small, the directional stability keeps turning the aircraft while the continuing bank angle maintains the sideslip and the yaw angle. This spiral gets continuously steeper and tighter until finally, if the motion is not checked, a steep, high-speed spiral dive results. The motion develops so gradually, however that it is usually corrected unconsciously by the pilot, who may not be aware that spiral instability exists. If the pilot cannot see the horizon, for instance because of clouds, he might not notice that he is slowly going into the spiral dive, which can lead into the graveyard spiral.

To be spirally stable, an aircraft must have some combination of a sufficiently large dihedral, which increases roll stability, and a sufficiently long vertical tail arm, which increases yaw damping. Increasing the vertical tail area then magnifies the degree of stability or instability.

The spiral dive should not be confused with a spin.[3]

a) Detection

While descending turns are commonly performed by pilots as a standard flight maneuvers, the spiral dive is differentiated from a descending turn owing to its feature of accelerating speed. It is therefore an unstable flight condition, and pilots are trained to recognize its onset and to implement recovery procedures safely and immediately. Without intervention by the pilot, acceleration of the aircraft will lead to structural failure of the airframe, either as a result of excess aerodynamic loading or flight into terrain. Spiral dive training therefore revolves around pilot recognition and recovery.[3]

b) **Recovery**

Spiral dive accidents are typically associated with visual flight (non-instrument flight) in conditions of poor visibility, where the pilot's reference to the visual natural horizon is effectively reduced, or prevented entirely, by such factors as cloud or darkness. The inherent danger of the spiral dive is that the condition, especially at onset, cannot be easily detected by the sensory mechanisms of the human body. The physical forces exerted on an airplane during a spiral dive are effectively balanced and the pilot cannot detect the banked attitude of the spiral descent. If the pilot detects acceleration, but fails to detect the banked attitude associated with the spiral descent, a mistaken attempt may be to recovery with mere back pressure (pitch-up inputs) on the control wheel. However, with the lift vector of the aircraft now directed to the centre of the spiral turn, this erred nose-up input simply tightens the spiral condition and increases the rate of acceleration and increases dangerous airframe loading. To successfully recover from a spiral dive, the lift vector must first be redirected upward (relative to the natural horizon) before backpressure is applied to the control column. Since the acceleration can be very rapid, recovery is dependent on the pilot's ability to quickly close the throttle (which is contributing to the acceleration), position the lift vector upward, relative to the Earth's surface before the dive recovery is implemented; any factor that would impede the pilot's external reference to the Earth's surface could delay or prevent recovery. The quick and efficient completion of these tasks is crucial as the aircraft can accelerate through maximum speed limits within only a few seconds, where the structural integrity of the airframe will be compromised.

For the purpose of flight training, instructors typically establish the aircraft in a descending turn with initially slow but steadily accelerating airspeed – the initial slow speed facilitates

the potentially slow and sometimes erred response of student pilots. The cockpit controls are released by the instructor and the student is instructed to recover. It is not uncommon for a spiral dive to result from an unsuccessful attempt to enter a spin, but the extreme nose-down attitude of the aircraft during the spin-spiral transition makes this method of entry ineffective for training purposes as there is little room to permit student error or delay.

All spiral dive recoveries entail the same recovery sequence: first, the throttle must be immediately closed; second, the aircraft is rolled level with co-ordinate use of ailerons and rudder; and third, backpressure is exerted smoothly on the control wheel to recover from the dive.[3]

3) Dutch roll

The second lateral motion is an oscillatory combined roll and yaw motion called Dutch roll, perhaps because of its similarity to an ice-skating motion of the same name made by Dutch skaters; the origin of the name is unclear. The Dutch roll may be described as a yaw and roll to the right, followed by a recovery towards the equilibrium condition, then an overshooting of this condition and a yaw and roll to the left, then back past the equilibrium attitude, and so on. The period is usually on the order of 3-15 seconds, but it can vary from a few seconds for light aircraft to a minute or more for airliners. Damping is increased by large directional stability and small dihedral and decreased by small directional stability and large dihedral. Although usually stable in a normal aircraft, the motion may be so slightly damped that the effect is very unpleasant and undesirable. In swept-back wing aircraft, the Dutch roll is solved by installing a yaw damper, in effect a special-purpose automatic pilot that damps out any yawing oscillation by applying rudder corrections. Some swept-wing aircraft have an unstable Dutch roll. If the Dutch roll is very lightly damped or unstable, the yaw damper becomes a safety requirement, rather than a pilot and passenger convenience. Dual yaw dampers are required and a failed yaw damper is cause for limiting flight to low altitudes, and possibly lower mach numbers, where the Dutch roll stability is improved.[2]

2.1.9 Displacement Autopilot

2.1.9.1 Longitudinal Displacement Autopilot

"The simplest form of autopilot, which is the type that first appeared in aircraft and is still being used in some of the older transport aircraft, is the displacement-type autopilot. This autopilot was designed to hold the aircraft in straight and level flight with little or no maneuvering capability. A block diagram such an autopilot is shown in figure (2-6).



Figure(2-6): Displacement autopilot of longitudinal motion

For this type of autopilot the aircraft is initially trimmed to straight and level flight, the reference aligned, and then the autopilot engaged. If the pitch attitude varies from the reference, a voltage $\mathbf{e}_{\mathbf{g}}$ is produced by the signal generator on the vertical gyro. This voltage is then amplified and fed to the elevator servo. The elevator servo can be electromechanical or hydraulic with an electrically operated valve. The servo then positions the elevator, causing the aircraft to pitch about the **Y** axis and so returning it to the desired pitch attitude".[5]

2.1.9.2 Type1 and Type0 System

"Block diagram of the type0 and type1 system are shown in figures (2-6) and (2-7) respectively. Difference between the type0 and type1 system is in the steady state error. In type0 system there is steady state error for unit step input, but in type1 system there is no such type of steady state error. In the type1system, there is one inner loop, this inner loop contains two blocks, one for the aircraft dynamics and other for the combined amplifier and elevator servo. For the internal loop, S(rg) is used as feedback whose value is tuned. In the outer loop, S(amp) is the outer loop gain with unity feedback. In the type0 system there is no need of the internal loop. To make the system type0 a differentiator is used with the aircraft dynamics, so in this case there is no need of S(rg), but the same autopilot is used for the both type of systems". [5]



Figure(2-7): Type (1) displacement autopilot of longitudinal motion

2.1.10 Lateral Displacement Autopilot

"AS most aircraft are spirally unstable, there is no tendency for the aircraft to return to its initial heading and roll angle after it has been disturbed from equilibrium by either a control surface deflection or a gust. Thus the pilot must continually make corrections to maintain a given heading. The early lateral autopilots were designed primarily to keep the wing level and hold the aircraft on a desired heading. A vertical gyro was used for the purpose of keeping the wing level, and a directional gyro was used for the heading reference. Figure(2-8) is a block diagram of such an autopilot. This autopilot had only very limited maneuvering capabilities. Once the references were aligned and the autopilot engaged, only small heading changes could be made. This was generally accomplished by changing the heading reference and thus yawing the aircraft through the use of the rudders to the new heading. Obviously such a maneuver was uncoordinated and practical only for small heading changes. Due to the lack of maneuverability and the light damping characteristic of the Dutch roll oscillation in high-performance aircraft, this autopilot is not satisfactory for our presentday aircraft. present-day lateral autopilots are much more complex. In most cases it is necessary to provide artificial damping of the Dutch roll. Also, to add maneuverability, provisions are

provided for turn control through the defection of the aileron, and coordination is achieved by proper signals to the rudder. In this discussion of lateral autopilots the damping of the Dutch roll is discussed first, followed by methods of obtaining coordination, and then the complete autopilot is examined".[5]



Figure (2-8): Displacement lateral autopilot

2.2 Stability and control

There are many ways for controlling an aircraft mechanism, such as classical controllers, adaptive controllers, neural controllers, etc.[6]

The first case study deal with fuzzy controller which is introduced by Lutfi Zadeh in 1973 and a fuzzy controller consists an input stage, a processing stage and an output stage. Input stage of a fuzzy controller turns inputs (such as sensors, switches etc.) to a suitable function and truth table values. These functions are called membership functions. In processing stage, a fuzzy controller generates a result for each rule and combine them. As a result of these stages, output stage converts them to a value which is going to be used in controller. Also it is being used for creating nonlinear controllers with some heuristic information. This heuristic information comes from an operator, who designs the controller, and it enters a decision making process and then it produces some outputs for controllers.[6]

by using Boeing747-E aerodynamic and stability derivatives' and all specifications need for modeling, then deal with design of the fuzzy controller as following steps:

- Fuzzy system as piecewise-linear interpolation.
- Parameter characterization and coding.
- Fuzzy rule tuning.
- Evaluation of design solution.

This case study deal with lateral autopilot for Boing747-E by using fuzzy control and give results.[6]



Evaluation: This method even if it is better in complex system design and multiple systems can be joined while creating it, it's have a little bit of complexity.[6]

The second case study used classic PID controller, after also modeling for Boeing747-E and used its transfer function then used PID tools for control and evaluation the design.[6,7]



Figure (2-10): System response when PID is applied

Evaluation: as it is seen, PID controller gives a little error on system for steady-state. Also there is no oscillation, which is better for a system, because if a system makes oscillation, it

shows that system responds your effects, moves your effect to a suitable place and stabilizes the system.[6,7]

Both **fuzzy** and **PID** give similar responses, sometimes PID may seem a little bit better, also PID controller is distinction by simplicity and reliability, availability of its tools and ease of construction.[6,7]

Thus the lateral autopilot for Boing747-E will used PID as controlling technique.[6,7]

3 Chapter Three: Calculation



3.1 Longitudinal Calculation

3.1.1 Longitudinal Motions

Develop the small-disturbance equations for longitudinal motions in standard state-variable form. Recall that the linearized equations describing small longitudinal perturbations from a longitudinal equilibrium state can be written:

$$\left[\frac{d}{dt} - X_u\right]u + g_0 \cos \Theta_0 \theta - X_\omega \omega = X_{\delta e} \delta_e + X_{\delta T} \delta_T$$
(3-1)

$$-Z_{u}u + \left[(1 - Z_{\dot{\omega}})\frac{d}{dt} - Z_{\omega} \right] \omega - \left[u_{0} + Z_{q} \right] q + g_{0} \sin\Theta_{0}\theta = Z_{\delta e}\delta_{e} + Z_{\delta T}\delta_{T}$$
(3-2)

$$-M_{u}u - \left[M_{\dot{\omega}}\frac{d}{dt} + M_{\omega}\right]\omega + \left[\frac{d}{dt} + M_{q}\right]q = M_{\delta e}\delta_{e} + M_{\delta T}\delta_{T}$$
(3-3)

If we introduce the longitudinal state variable vector

$$X = [u w q \mu]^T$$
(3-4)

and the longitudinal control vector

$$\eta = [\delta e \ \delta_T]^T \tag{3-5}$$

these equations are equivalent to the system of first-order equations

$$\ln \mathbf{X} = A_n \mathbf{X} + B_n \eta \tag{3-6}$$

Where \mathbf{x} represents the time derivative of the state vector x, and the matrices appearing in this equation are:
$$\boldsymbol{A_n} = \begin{pmatrix} X_u & X_\omega & 0 & -g_0 \cos \Theta_0 \\ Z_u & Z_\omega & u_0 + Z_q & -g_0 \sin \Theta_0 \\ M_u & M_\omega & M_q & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}$$
(3-7)

$$\mathbf{I}_{n} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 - \mathbf{Z}_{\dot{\omega}} & 0 & 0 \\ 0 & - \mathbf{M}_{\dot{\omega}} & 1 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}$$
(3-8)

$$\mathbf{B}_{n} = \begin{pmatrix} X_{\delta e} & X_{\delta T} \\ Z_{\delta e} & Z_{\delta T} \\ M_{\delta e} & M_{\delta T} \\ 0 & 0 \end{pmatrix}$$
(3-9)

The inverse of I_n

$$\mathbf{I_n}^{-1} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & \frac{1}{1 - Z_{\dot{\omega}}} & 0 & 0 \\ 0 & \frac{M_{\dot{\omega}}}{1 - Z_{\dot{\omega}}} & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$
(3-10)

As premultiplying Eq. (6) by I_n^{-1} gives the standard form:

 $\dot{x} = Ax + B\eta \tag{3-11}$

Where :

А	is the state matrix
В	is the input matrix
X	is the state vector
η	is the control vector

The A and B consist of aircraft's dimensional stability and control derivatives.

$$A = \begin{pmatrix} X_{u} & X_{\omega} & 0 & -g_{0} \cos \theta_{0} \\ \frac{Z_{u}}{1-Z_{\dot{\omega}}} & \frac{Z_{\omega}}{1-Z_{\dot{\omega}}} & \frac{u_{0}+Z_{q}}{1-Z_{\dot{\omega}}} & \frac{-g_{0} \sin \theta_{0}}{1-Z_{\dot{\omega}}} \\ M_{u} + \frac{M_{\dot{\omega}}Z_{u}}{1-Z_{\dot{\omega}}} & M_{\omega} + \frac{M_{\dot{\omega}}Z_{u}}{1-Z_{\dot{\omega}}} & M_{q} + \frac{(u_{0}+Z_{q})M_{\dot{\omega}}}{1-Z_{\dot{\omega}}} & \frac{-M_{\dot{\omega}}g_{0} \sin \theta_{0}}{1-Z_{\dot{\omega}}} \\ 0 & 0 & 1 & 0 \end{pmatrix}$$
(3-12)

$$\mathbf{B} = \begin{pmatrix} X_{\delta e} & X_{\delta T} \\ \frac{Z_{\delta e}}{1 - Z_{\dot{\omega}}} & \frac{Z_{\delta T}}{1 - Z_{\dot{\omega}}} \\ M_{\delta e} &+ \frac{M_{\dot{\omega}} Z_{\delta e}}{1 - Z_{\dot{\omega}}} & M_{\delta T} + \frac{M_{\dot{\omega}} Z_{\delta T}}{1 - Z_{\dot{\omega}}} \\ 0 & 0 \end{pmatrix}$$
(3-13)

Note that:

$$Z_{\dot{\omega}} = \frac{QS\bar{c}}{2mu_0^2} C_{Z_{\dot{\alpha}}} = -\frac{1}{2\mu} C_{L_{\dot{\alpha}}}$$
(3-14)

$$Z_{q} = \frac{QS\bar{c}}{2mu_{0}} C_{Z_{q}} = -\frac{u_{0}}{2\mu} C_{L_{q}}$$
(3-15)

Where:

 μ is aircraft mass parameter is typically large (on the order of 100), it is common to neglect $Z_{\dot{\omega}}$ with respect to unity and to neglect Z_q relative to u_0 , in which case the matrices A and B can be approximated as:

$$A = \begin{pmatrix} X_{u} & X_{\omega} & 0 & -g_{0} \cos \theta_{0} \\ Z_{u} & Z_{\omega} & u_{0} & -g_{0} \sin \theta_{0} \\ M_{u} + M_{\omega} Z_{u} & M_{\omega} + M_{\omega} Z_{\omega} & M_{q} + u_{0} M_{\omega} & -M_{\omega} g_{0} \sin \theta_{0} \\ 0 & 0 & 1 & 0 \end{pmatrix}$$
(3-16)
$$B = \begin{pmatrix} X_{\delta e} & X_{\delta T} \\ Z_{\delta e} & Z_{\delta T} \\ M_{\delta e} + M_{\omega} Z_{\delta e} & M_{\delta T} + M_{\omega} Z_{\delta T} \\ 0 & 0 \end{pmatrix}$$
(3-17)

This is the approximate form of the linearized equations for longitudinal motions as they appear in many texts.

The various dimensional stability derivatives appearing in Equations. (3-16) and (3-17) are related to their dimensionless aerodynamic coefficient in Table (3-1)

 Table (3-1) : The various dimensional stability derivatives related to their dimensionless aerodynamic coefficient in a longitudinal motion

Variable	X	Z	М
U	$X_u = \frac{QS}{mu_0} \left[2C_{X_0} + C_{X_u} \right]$	$Z_u = \frac{QS}{mu_0} \left[2C_{Z_0} + C_{Z_u} \right]$	$M_u = \frac{QS\bar{c}}{I_y u_0} C_{m_u}$
ω	$X_{\omega} = \frac{QS}{mu_0} C_{X_{\alpha}}$	$Z_{\omega} = \frac{QS}{mu_0} C_{Z_{\alpha}}$	$M_{\omega} = \frac{QS\bar{c}}{I_{y}u_{0}} C_{m_{\alpha}}$
ώ	$X_{\dot{\omega}} = 0$	$Z_{\dot{\omega}} = \frac{QS\bar{c}}{2mu_0^2} C_{Z_{\dot{\alpha}}}$	$M_{\dot{\omega}} = \frac{QS\bar{c}^2}{2I_y {u_0}^2} C_{m_{\dot{\alpha}}}$
Q	$X_q = 0$	$Z_q = \frac{QS\bar{c}}{2mu_0} C_{Z_q}$	$M_q = \frac{QS\bar{c}^2}{2I_y u_0} C_{m_q}$

We illustrate this response using the stability derivatives for the Boeing 747 aircraft at its Mach 0.5 powered approach configuration at standard 20,000 ft conditions. To illustrate typical longitudinal behavior response, we need the following vehicle parameters :

U	158 m/s	S	$510 m^2$
ρ	$0.088032 \text{ kg/}m^3$	М	250000 kg
Ē	8.3 m	Iy	41.35 * 10 ⁶ kg.m ²

 Table (3-2) :specification of Boeing 747-E

and the relevant aerodynamic coefficients are:

 Table (3-3): Aerodynamic coefficients

CL	0.680	$C_{m_{\alpha}}$	-1.146
C _D	0.0393	C _{mà}	-3.35
Θ ₀	0	<i>C</i> _{<i>m</i>_q}	-20.7
C _{Lα}	4.67	С _{<i>m</i>м}	0.121
C _{Lq}	5.13	$C_{D_{\alpha}}$	0.366
C _L _ά	6.35	C _{LM}	-0.0875

These values correspond to the following dimensional stability derivatives

Table (3-4): Dimensional stability derivatives

X _u	-0.003	Zu	-0.07
Χ _ω	0.078	Ζ _ω	-0.433
M _u	0.00008	Zq	-1.95
Μ _ω	-0.006	Z _ŵ	Neglect
Mq	-0.421	M _ώ	-0.0004

$$A = \begin{pmatrix} -0.003 & 0.078 & 0 & -9.81 \\ -0.07 & -0.433 & 158 & 0 \\ 0.000108 & -0.00617 & -0.4842 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}$$

3.1.1.1 Characteristic Equation

Given square matrix A the equation

$$s^{4} + 0.91132 s^{3} + 1.1028 s^{2} + 0.0056507 s + 0.0043911 = 0$$
(3-18)

Equation (3-18) is called characteristic equation of matrix A.

 $|A - \lambda I|$ denotes the determinant of the argument (square) matrix , and I is identity matrix its dimension= dimension of matrix A

The roots of characteristic equation.(3-18) are called the eigen values of the matrix A and are usually denoted by

 r_1, r_2, \ldots, r_n where n is the number of columns or rows of matrix A

3.1.1.2 Aircraft Characteristic Equation

It is polynomial equation which is fourth order in S- domain as follow

$$as^4 + bs^3 + cs^2 + ds + e = 0 (3-19)$$

Where coefficients a, b, c, d and e are real quantities.

Equation(3-19)can be written as:

$$(s^{2} + 2\zeta\omega_{n}s + \omega_{n}^{2})_{sp} (s^{2} + 2\zeta\omega_{n}s + \omega_{n}^{2})_{p} = 0$$
(3-20)



For stable oscillation type of motion, the roots of these characteristic equation on S-plan.

Figure (3-11) :General Root Locus of longitudinal modes



Figure (3-12) :Root Locus of Boeing 747-E longitudinal modes

The characteristic equation for longitudinal mode usually factorizes into two pairs of complex roots:

- i) The high frequency pair of roots describes the short period pitching oscillation
- ii) The low frequency pair describes the phugoid oscillation

Solution of equation (3-20) gives four roots each root can be represented in following form:

$$\alpha \pm j \,\omega_{\rm d} = \omega_{\rm n} \zeta \pm j \,\omega_{\rm n} \sqrt{1 - \zeta^2} \tag{3-21}$$

Where:

 ζ =damping ratio ω_n =undamped natural frequency

The eigen values (known also as roots) obtained can be used to determine:

 The time to double amplitude (for dynamically unstable system) or time to half amplitude (for dynamically stable system)

$$t_{double} or t_{1/2} = \frac{0.693}{|\eta|}$$
(3-22)

2) Period

$$period = \frac{2\pi}{\omega_d} \tag{3-23}$$

Note:

Equations (3-22) & (3-23) can be used for both phugoid & short period motion.

3.1.1.3 Dynamic Stability of the System

An aircraft may be said to be dynamically **stable** it all its eigen values, being real, have negative values, or if the be complex, have negative real part. And zero or positive values of the real part of any complex eigen values mean that aircraft will be dynamically **unstable**.

The complex eigen values of Boeing 747-E:

$$\lambda$$
 1,2= -0.4547 ± 0.9436i
 λ 3,4 = -0.0009 ± 0.0633i

This aircraft is dynamically stable.

The first two pair of roots are for short period oscillation mode and the other pair for phugoid oscillation

$$(\boldsymbol{\omega}_n)_{short} = 1.048 \text{ rad/s}$$
 $(\boldsymbol{\omega}_n)_{phugoid} = 0.0638 \text{ rad/s}$

3.1.1.4 Longitudinal Modes of Typical Aircraft

The natural response of most aircraft to longitudinal perturbations typically consists of two under damped oscillatory modes having rather different time scales. One of the modes has a relatively short period and is usually quite heavily damped; this is called the short period mode. The other mode has a much longer period and is rather lightly damped; this is called the phugoid mode.



Figure (3-13) Response of longitudinal motion

3.1.2 Longitudinal Displacement autopilot

This autopilot was designed to hold the aircraft in straight and level flight with little or no maneuvering capability. A block diagram of Boeing 747-E longitudinal autopilot is shown in figure (3-4).



Figure (3-14): Displacement autopilot of Boeing 747-E

And the displacement autopilot for Boeing 747-E with pitch rate feedback added for damping as show in figure (3-5):



Figure (3-15): Block diagram for the displacement autopilot with pitch rate feedback added for damping

3.1.2.1 Inner Loop Transfer Function

In Automatic control we derived the transfer function of a simple feedback system. In the figure below a feedback system similar to our inner loop is shown.



Figure (3-16): Block diagram of a similar, simple feedback system

By simplifying the inner loop transfer function:

$$\frac{\theta}{e_a} = \frac{12.51 \, S + 3.17}{S^3 + 10.99 \, S^2 + 11.13 \, S + 12.26 + (12.51 \, S + 3.17) S_{rg}} \tag{3-24}$$

The root locus of the inner loop is drawn as follows:



Figure (3-17): Root Locus Diagram for Inner Loop

3.1.2.2 Outer Loop Transfer Function



Figure (3-18): Block diagram of the outer loop

Transfer function of the outer loop, $\frac{\theta}{\theta_{ref}}$ is found as in the Equation (3-25)

θ	$(12.51 S + 3.17) S_{amp}$
$\overline{\theta_{ref}}$	$\frac{1}{S[S^3+10.99S^2+11.13S+12.26+(12.51S+3.17)S_{rg}]+(12.51S+3.17)S_{amp}}$

(3-25)

The root locus of the outer loop is drawn as follows:



Figure(3-19): Root Locus Diagram for Outer Loop

3.1.3 Longitudinal simulation



Figure (3-20): Block diagram of simulation for Boeing 747-E longitudinal autopilot





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4									
2									
2									
1									
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0	1	2	3 4	1	5 1	3	7 I	3	9 10

Figure (3-22): The response of pitch rate($\dot{\theta}$) for Boeing 747-E at 20,000 ft



Figure (3-23): The response of elevator deflection (δ_e) for Boeing 747-E at 20,000 ft

3.1.4 Longitudinal control

3.1.4.1 Introduction

No adopt, the adding of controller to the pitch attitude autopilot improve the performance of the aircraft specially at longitudinal motion. This improvement can be done by different procedures but we found by assistant with graphical methods in Matlab, the best way to increase reliability of our aircraft system, adding the PD controller with suitable calculated gain.

3.1.4.2 controller Selection

Based upon previous procedures about different controllers, the optimum proposed controller that have open loop transfer function as:

$$G_c(s) = K_p + K_d S = 5 + 4S \tag{3-26}$$

The contribution of this controller upon the aircraft longitudinal channel was improving the system response that can be seen obviously in decreasing the overall specifications comparing with the system before adding the PD controller. It is effected in the specifications of the system. The setting time became very short and more convenient to the aircraft system and users. Also the decrease of rise time and overshoot in input step response as shown in preceding figures.

The overall transfer function of the aircraft with selected controller is

$$G_c(s). G_{(A/C)}(s) = \frac{(-1.251 \, s - 0.317)(5 + 4 \, s)}{s(s^2 + 0.99 \, s + 1.226)}$$
(3-27)

This can be represented by a block diagram as in figure (3-14).



Figure (3-24): Displacement longitudinal autopilot of Boeing 747-E with PD controller

From the previous block diagram was to improve the positions (increase stability) of phugoid pole and shows through the root locus in below



Figure (3-25): Root Locus of Boeing 747-E longitudinal modes after adding the PD controller

Also the response of longitudinal motion was improving that can be seen obviously in decreasing the overall specifications by adding the PD controller. Where the response up to steady state error in less time.



Figure (3-26): Response of longitudinal motion after adding the PD controller

3.2 Lateral Calculation

3.2.1 Lateral/Directional Motions

Develop the small-disturbance equations for lateral/directional motions in standard statevariable form. Recall that the linearized equations describing small lateral/directional perturbations from a longitudinal equilibrium state can be written:

$$\left[\frac{d}{dt} - Y_{\nu}\right]\nu - Y_{p}p + \left[u_{0} + Y_{r}\right]r - g_{0}\cos\Theta_{0}\phi = Y_{\delta r}\delta_{r}$$
(3-28)

$$-L_{\nu}\nu + \left[\frac{d}{dt} - L_{p}\right]p - \left[\frac{l_{xz}}{l_{x}}\frac{d}{dt} + L_{r}\right]r = L_{\delta r}\delta_{r} + L_{\delta a}\delta_{a}$$
(3-29)

$$-N_{\nu}\nu - \left[\frac{I_{xz}}{I_z}\frac{d}{dt} + N_p\right]p + \left[\frac{d}{dt} - N_r\right]r = N_{\delta r}\delta_r + N_{\delta a}\delta_a$$
(3-30)

Using a procedure similar to the longitudinal case, we can develop the equations of motion for the lateral dynamics.

If we introduce the lateral/directional state variable vector

$$X = [v \ p \ \emptyset \ r]^T \tag{3-31}$$

The lateral/directional control vector

$$\eta = [\delta r \ \delta_a]^T \tag{3-32}$$

These equations are equivalent to the system of first-order equations

$$\mathbf{X} = \mathbf{A}\mathbf{X} + \mathbf{B}\,\mathbf{\eta} \tag{3-33}$$

Where:

X represents the time derivative of the state vector \mathbf{x}

$$A = \begin{pmatrix} Y_{v} & Y_{p} & g_{0} \cos \Theta_{0} & Y_{r} - u_{0} \\ \frac{L_{v} + i_{x}N_{v}}{1 - i_{x}i_{z}} & \frac{L_{p} + i_{x}N_{p}}{1 - i_{x}i_{z}} & 0 & \frac{L_{r} + i_{x}N_{r}}{1 - i_{x}i_{z}} \\ 0 & 1 & 0 & 0 \\ \frac{N_{v} + i_{z}L_{v}}{1 - i_{x}i_{z}} & \frac{N_{p} + i_{z}L_{p}}{1 - i_{x}i_{z}} & 0 & \frac{N_{r} + i_{z}L_{r}}{1 - i_{x}i_{z}} \end{pmatrix}$$
(3-34)

$$\mathbf{B} = \begin{pmatrix} Y_{\delta_r} & 0 \\ \frac{L_{\delta_r} + i_x N_{\delta_r}}{1 - i_x i_z} & \frac{L_{\delta_a} + i_x N_{\delta_a}}{1 - i_x i_z} \\ 0 & 0 \\ \frac{N_{\delta_r} + i_z L_{\delta_r}}{1 - i_x i_z} & \frac{N_{\delta_a} + i_z L_{\delta_a}}{1 - i_x i_z} \end{pmatrix}$$
(3-35)

For most flight vehicles and situations, the ratios i_x and i_z are quite small. Neglecting these quantities with respect to unity allows us to write the **A** and **B** matrices for lateral directional motions as:

$$\mathbf{A} = \begin{pmatrix} Y_{v} & Y_{p} & g_{0} \cos \Theta_{0} & Y_{r} - u_{0} \\ L_{v} & L_{p} & 0 & L_{r} \\ 0 & 1 & 0 & 0 \\ N_{v} & N_{p} & 0 & N_{r} \end{pmatrix}$$
(3-36)
$$\mathbf{B} = \begin{pmatrix} Y_{\delta_{r}} & 0 \\ L_{\delta_{r}} & L_{\delta_{a}} \\ 0 & 0 \\ N_{\delta_{r}} & N_{\delta_{a}} \end{pmatrix}$$
(3-37)

The various dimensional stability derivatives $(L_v, N_p, Y_{\delta_r},...)$ appearing in above equations are related to their dimensionless aerodynamic coefficients as follows

 Table (3-5): The various dimensional stability derivatives related to their dimensionless aerodynamic coefficient in a lateral motion

Variable	Y	L	N
V	$Y_{\nu} = \frac{QS}{mu_0} C_{\gamma_{\beta}}$	$L_{\nu} = \frac{QSb}{I_{x}u_{0}} C_{l_{\beta}}$	$N_{\nu} = \frac{QSb}{I_z u_0} C_{n_{\beta}}$
р	$Y_p = \frac{QSb}{2mu_0} C_{y_p}$	$L_p = \frac{QSb^2}{2I_x u_0} C_{l_p}$	$N_p = \frac{QSb^2}{2I_z u_0} C_{n_p}$
R	$Y_r = \frac{QSb}{2mu_0} C_{y_r}$	$L_r = \frac{QSb^2}{2I_x u_0} C_{l_r}$	$N_r = \frac{QSb^2}{2I_z u_0} C_{n_r}$

3.2.1.1 Modes of Typical Aircraft

The natural response of most aircraft to lateral/directional perturbations typically consists of:

One damped oscillatory mode This mode has a relatively short period and can be relatively lightly damped, especially for swept-wing aircraft; this is called the **Dutch Roll mode**. And two exponential modes One of which is usually very heavily damped and represents the response of the aircraft primarily in roll; it is called the **rolling mode**. The second exponential mode, called the **spiral mode**, can be either stable or unstable, but usually has a long enough time constant that it presents no difficulty for piloted vehicles, even when it is unstable.

We illustrate this response again using the stability derivatives for the Boeing 747 aircraft at its Mach 0.5 powered approach configuration at standard 20,000 ft conditions. This is the same vehicle and trim condition used to illustrate typical longitudinal behaviour. In addition, for the lateral/directional response we need the following vehicle parameters

U	158 m/s	S	$510 m^2$
Р	0.088032 kg/m^3	М	250000 kg
Ē	8.3 m	I _x	$18.6 * 10^6 \text{ kg.} m^2$
I _z	58*10 ⁶ kg.m ²	I _{xz}	$1.2*10^{6}$ kg. m^{2}
В	59.75 m	Q	8667 N/m ²

Table(3-6) :	specification	of Boeing	747-E
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and the aerodynamic derivatives are:

C _y	-0.90	Clp	0.323-
C _{lr}	0.212	C _l	-0.193
C _{nr}	-0.278	C _{np}	-0.0687
C _n	0.147		

 Table (3-7): The aerodynamic coefficient

These values correspond to the following dimensional stability derivatives:

Table (3-8):	The dimensional	stability	derivatives
---------------------	-----------------	-----------	-------------

Y _v	-0.1007	L_v	-0.0176
N _v	0.00497	L _p	-0.8766
Y _p	-0.281	N _p	-0.0694
Y _r	0.443	L _r	0.5754
N _r	-0.281		

and the dimensionless product of inertia factors are:

$$i_x = \frac{i_{xz}}{i_x} = 0.0645$$
 and $i_z = \frac{i_{xz}}{i_z} = 0.0207$

Using these values, the plant matrix is found to be

$$A = \begin{pmatrix} -0.1007 & -0.2810 & 9.8100 & -157.5570 \\ -0.0176 & -0.8766 & 0 & 0.5754 \\ 0 & 1.0000 & 0 & 0 \\ 0.0050 & -0.0694 & 0 & -0.2810 \end{pmatrix}$$

The characteristic equation is given by:

 $|A - \lambda I| = s^4 + 1.2592 s^3 + 1.1897 s^2 + 1.0833 s + 0.215 = 0$

And its roots are:

 $\lambda DR = -0.0812 \pm 0.9877 i$ $\lambda roll = -1.0766$ $\lambda spiral = -0.0194$

All its eigen values (roots) being real, have negative values, or be complex, have negative real part. Therefore the aircraft is **Stable**, but there is one very slow pole.

There are three modes, but they are a lot more complicated than the longitudinal case.

Table (3-9): The lateral modes

Slow mode	-0.0194	Spiral Mode	slow, often unstable.
Fast real	-1.0766	Roll Damping	well damped.
Oscillatory	-0.0812± 0.9877 i	Dutch Roll	damped oscillation in yaw, that couples into roll.

3.2.1.1.1 The damping ratio ,undamped natural frequency of the Dutch Roll mode

Assume the two roots can be represented as follows:

$$\alpha \pm j \,\omega_{\rm d} = \omega_{\rm n} \zeta \pm j \,\omega_{\rm n} \sqrt{1 - \zeta^2} \tag{3-38}$$

Damping ratio:

$$\zeta_{DR} = \sqrt{\frac{1}{1 + (\frac{\eta}{\xi})^2}} = \sqrt{\frac{1}{1 + (\frac{0.9877}{0.0812})^2}} = 0.0819$$
(3-39)

where ξ and η are the real and imaginary parts of the respective roots, and the undamped natural frequency of the mode is

$$\omega_{DR} = \frac{-\xi}{\zeta} = \frac{0.0812}{0.0819} = 0.9915 \, Sec^{-1} \tag{3-40}$$

The period of the Dutch Roll mode is then given by:

$$T_{DR} = \frac{2\pi}{\omega n \sqrt{1-\zeta^2}} = \frac{2\pi}{0.9915\sqrt{1-0.0819^2}} = 6.355 \text{ Sec}$$
 (3-41)

And the number of cycles to damp to half amplitude is

$$N_{1/2_{DR}} = \frac{\ln 2}{2\pi} \frac{\sqrt{1-\zeta^2}}{\zeta} = \frac{\ln 2}{2\pi} \frac{\sqrt{1-0.0819^2}}{0.0819} = 1.343$$
(3-42)

Thus, the period of the Dutch Roll mode is seen to be on the same order as that of the longitudinal short period mode, but is much more lightly damped.

3.2.1.1.2 The times to damp to half amplitude for the rolling and spiral modes

The times to damp to half amplitude for the rolling and spiral modes are seen to be

$$t_{1/2_{roll}} = \frac{Ln 2}{-\zeta roll} = \frac{Ln 2}{1.0766} = 0.644 \text{ Sec}$$
 and
$$t_{1/2_{spiral}} = \frac{Ln 2}{-\zeta spiral} = \frac{Ln 2}{0.0194} = 35.73 \text{ Sec}$$

The responses characteristic of these aircraft is illustrated in following figure:



Figure (3-27): The response of lateral motion for Boeing 747-E



The responses characteristic of these three mode are illustrated in following figures:

Figure (3-29): Spiral mode



Figure (3-30): Dutch Roll

3.2.2 Lateral autopilot

As continues work on the autopilot of the aircraft, after longitudinal autopilot we will work on the lateral autopilot. This autopilot had only very limited maneuvering capabilities, a block diagram of Boeing 747-E lateral autopilot is shown in figure (3-21).



Figure (3-31): Basic lateral autopilot

3.2.2.1 Damping of Dutch roll

As previously mentioned that the rudder excites primarily the Dutch roll mode; the Dutch roll that is observed in yow rate and side slip response from an aileron deflection is caused by the yawing moment resulting from the aileron deflection. For these reasons the usual method of damping the Dutch roll is to detect the yaw rate with a rate gyro and use this signal to deflect the rudder. Figure below is a block diagram of the Dutch roll damper. The washout circuit produces an output only during the transient period. If the yaw rate signal did not go to zero in the steady state, then for a positive yaw rate, for instance, the output of the yaw rate gyro would produce a positive rudder deflection. This would result in an uncoordinated maneuver and require a larger pilot's rudder input to achieve coordination.



Figure (3-32) : Block diagram of Dutch roll damper



Figure (3-33): Block diagram of the Dutch roll damper for the root locus study

Where:

$$[TF]_{(A/C)[\delta_r:r]} = \frac{-0.577 \, S^2 - 0.0519 \, S - 0.0923}{S^3 + 0.1814 \, S^2 + 0.98614 \, S + 0.0191}$$
(3-43)

And the yaw rate gyro:

 $S_{(yrg)} = 1.04 \text{ volt/(deg/sec)}$

Then a transfer function of this block diagram are:

$$[TF]_{(A/C)[r_c:r]} = \frac{-1.04\,S^5 - 4.349\,S^4 - 1.78\,S^3 - 4.122\,S^2 - 0.07946\,S}{S^5 + 5.181\,S^4 + 8.293\,S^3 + 5.891\,S^2 + 4.424\,S + 0.0764}$$
(3-44)



From above transfer function produce the root locus in the figure (3-24):

Figure (3-34): Root locus for the Dutch roll damper for τ of the washout circuit equal to 1 sec

3.2.3 Lateral simulation



Figure (3-35): Block diagram of simulation for Boeing 747-E lateral autopilot

The figures below shows the results of a computer simulation of the aircraft with the Dutch roll damper.



Figure (3-36): Response of the aircraft (r) with Dutch roll damping for $S_{(yrg)} = 1.04$ volt/(deg/sec) for a pulse aileron deflection



Figure (3-37): Response of the aircraft (δ_r) with Dutch roll damping for $S_{(yrg)} = 1.04$ volt/(deg/sec) for a pulse aileron deflection

3.2.4 Lateral control

We can stabilize or modify the lateral dynamics using a variety of feedback architectures.

And we show on figure below a block diagram of this yaw damper, using proportional feedback.



Figure(3- 38): Block diagram of the Dutch roll damper with controller

The transfer function of the aircraft dynamic in the block are:

$$[TF]_{(A/C)[\delta_r:r]} = \frac{-0.577 \, S^2 - 0.0519 \, S - 0.0923}{S^3 + 0.1814 \, S^2 + 0.98614 \, S + 0.0191}$$
(3-45)

Note that:

The gain of the plant is negative $(K_{plant} < 0)$, so if $k_r < 0$, then $K = K_{plant} k_r > 0$, so must draw a root locus (negative feedback).



Figure(3- 39): lateral autopilot: r to δ_r with $k_r > \ 0$



Figure (3-40): lateral autopilot: r to δ_r with $k_r < \ 0$

Root locus with $k_r < 0$ looks pretty good as we have authority over the four poles. And at $k_r = -1.6$ results in a large increase in the Dutch roll damping mode have combined into a damped oscillation.

Also the response of Dutch roll damper was improving that can be seen obviously in decreasing the overall specifications by adding the controller. Where the response up to steady state error in less time.



Figure (3-31): Response of the aircraft (r) with Dutch roll damping after adding controller

3.2.5 The lateral Evaluation

3.2.5.1 Lateral Autopilot Evaluation for Boeing 747-E by Root-locus

To evaluation the lateral autopilot will be the highlight of the Dutch roll damper because the Dutch roll oscillation is a coupled lateral-directional oscillation. And this evaluation will be through the use of Root-locus.

The Root locus for Dutch roll damper is drawn by using MATLAB as the feedback controller k_r ; k_r is decreased from 1 to -10. The value of rate gyro is 0.1, the root locus for Dutch roll damper of different values of feedback controller is shown below.



Figure (3-42): Root locus of Dutch roll damper at k_r equal to 1



Figure (3-43): Root locus of Dutch roll damper at k_r equal to -1



Figure (3-44): Root locus of Dutch roll damper at k_r equal to -1.6

53



Figure (3-45): Root locus of Dutch roll damper at k_r equal to -2



Figure (3-46): Root locus of Dutch roll damper at k_r equal to -5



Figure(3- 47): Root locus of Dutch roll damper at k_r equal to -10

Evaluation:

To evaluate the response, it can be clearly seen that it was selected various value of negative gain with observing the root locus.

It was noted that when the negative gain increased poles move to left, but there is a certain value that's run over it will case overshooting in transit response.

4 Chapter Four: Results

4.1 Longitudinal Result

4.1.1 longtidunal motion

Table (4-1) : Aerodynamic coefficients

CL	0.680	$C_{m_{lpha}}$	-1.146
C _D	0.0393	C _{mà}	-3.35
Θ ₀	0	$C_{m_{q}}$	-20.7
$C_{L_{lpha}}$	4.67	<i>C</i> _{<i>m</i>_M}	0.121
C _{Lq}	5.13	$C_{D_{\alpha}}$	0.366
$C_{L_{\dot{\alpha}}}$	6.35	C _{LM}	-0.0875

Table (4-2) : Dimensional stability derivatives

Xu	-0.003	Zu	-0.07
Χ _ω	0.078	Ζ _ω	-0.433
M _u	0.00008	Zq	-1.95
Μ _ω	-0.006	Ζ _ώ	Neglect
Mq	-0.421	Μ _ώ	-0.0004

Table (4-3) : The roots and natural frequency

Roots of short period	-0.4547 ± 0.9436i	(ω _n) _{short}	1.048 rad/s
Roots of long period	$-0.0009 \pm 0.0633i$	$(\boldsymbol{\omega}_n)_{phugoid}$	0.0638 rad/s



Figure(4- 48): Root Locus of Boeing 747-E longitudinal modes



Figure (4-49): Response of longitudinal motion
4.1.2 Longitudinal Displacement Autopilot







Figure(4- 51): Root Locus Diagram for Outer Loop

4.1.3 Longitudinal Simulation

5.							
4							
3							
50 1	2 3	4	 5 6	6	,	3	10

Figure (4-52):The response of pitch angle (θ) for Boeing 747-E at 20,000 ft



Figure (4-53):The response of pitch rate ($\dot{\theta}$) for Boeing 747-E at 20,000 ft



Figure (4-54): The response of elevator deflection (δ_e) for Boeing 747-E at 20,000 ft

4.1.4 Longitudinal Control



Figure(4- 55): Root Locus of Boeing 747-E longitudinal modes after adding the PD controller



Figure (4-56): Response of longitudinal motion after adding the PD controller

4.2 Lateral/Directional Result

4.2.1 Lateral/Directional Motions

$C_{y_{\beta}}$	-0.90	Clp	0.323-
C _{lr}	0.212	$C_{l_{eta}}$	-0.193
C_{n_r}	-0.278	C_{n_p}	-0.0687
C _{n_β}	0.147		

Table (4-4): The aerodynamic coefficient

 Table (4-5): The dimensional stability derivatives

Υ _ν	-0.1007	L_v	-0.0176
N _v	0.00497	L _p	-0.8766
Y _p	-0.281	N _p	-0.0694
Y _r	0.443	L _r	0.5754
N _r	-0.281		

 Table (4-6): The lateral modes

Slow mode	-0.0194	Spiral Mode	slow, often unstable.
Fast real mode	-1.0766	Roll Damping	well damped.
Oscillatory mode	-0.0812± 0.9877 i	Dutch Roll	damped oscillation in yaw, that couples into roll.

Table (4-7): The damping ratio ,undamped natural frequency, the period, and the

number of cycles to damp to half amplitude of the Dutch Roll mode

ζ _{DR}	0.0819	ω _{DR}	0.9915 Sec ⁻¹
T _{DR}	6.355 Sec	N _{1/2_{DR}}	1.343

 Table (4-8) :The times to damp to half amplitude for the rolling and spiral modes

t _{1/2_{roll}}	0.644 Sec	$t_{1/2_{spiral}}$	35.73 Sec



Figure (4-57): The response of lateral motion for Boeing 747



Figure (4-58): Rolling mode







Figure (4-60):Dutch Roll

4.2.2 Lateral Autopilot



figure (4-61): Root locus for the Dutch roll damper for τ of the washout circuit equal to 1 sec

4.2.3 Lateral Simulation

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Figure (4-62):Response of the aircraft (r) with Dutch roll damping for $S_{(yrg)} = 1.04$ volt/(deg/sec) for a pulse aileron deflection

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2									
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Figure (4-63): Response of the aircraft (δ_r) with Dutch roll damping for $S_{(yrg)} = 1.04$ volt/(deg/sec) for a pulse aileron deflection

4.2.4 Lateral Control



Figure (4-64): lateral autopilot: r to δ_r with $k_r < \ 0$

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Figure (4-65): Response of the aircraft (r) with Dutch roll damping after adding controller

5 Chapter Five: Discussion

5.1 Longitudinal Discussion

The graph shows Root Locus of Boeing 747-E longitudinal modes ,it can be clearly seen that the system(longitduinal motion) is conditionly stable.

The longitudinal motion have four poles two for short period and the other two for long period (phugoid), short period poles is stable and long period poles its clearly seen its poorly stable which are locates nearly zero.

The system called contdionly stable and its not desirble since if the gain drops beyond the critical value for some reason, the system becomes unstable .

This graph shows Response of longitudinal motion (short response); it can be clearly see that the Transient response is not satisfactory (due to short mode).

Although longitudinal motion of the system is stable (from its root locus) but the Transient response is not satisfactory expressed in the Response of the longitudinal motion,

Overall its need to make its derisible as possible by reshaped the root locus by using PD controller.





The graph describes The response of pitch angle (θ) for Boeing 747-E at 20,000 ft, it can be clearly seen that the Transient response is satisfactory. This amendment obtained in the response due to adding an inner feed back loop utilizing a rate gyro.	
The graph describes The response of pitch rate $(\dot{\theta})$ for Boeing 747-E at 20,000 ft it can be seen that the Transient response is satisfactory but Steady-state error is too large (control requirement for longitudinal motion).	
The graph describes The response of elevator deflection (δ_e) for Boeing 747-E at 20,000 ft, it can be clearly seen that the response suffering down overshoot (need control to make improvement to its specifications).	

The graph shows Root Locus of Boeing 747-E longitudinal modes after adding the PD controller, it can be clearly seen that the system(longitudinal motion) is stable.

There are four poles two for short period and the other two for long period (phugoid), short period poles is stable and long period poles also here is stable(phugoid mode is stable) that's due to using PD controller .

This root locus diagram is results of reshaped a root locus of longtidinal motion(befor adding controller) to get satisfactory Transient response with satisfactory steady-state error.

Root Locus <u>*</u>€ Step Response -4.3 -4.4 -45 -46 (pad)

The graph shows Response of longitudinal motion after adding the PD controller; it can be clearly see that the Transient response is satisfactory (due using PD controller or inner loop) satisfactory steady state error.

the response is desirable (satisfactory Transient response and steady state error) that's as results of increasing the damping by using (inner feedback loop) and using PD controller.



5.2 Lateral Discussion

The graph describes response of lateral motion for Boeing 747-E (yaw rate), it can be clearly seen that the response has obvious oscillatory.

The response is lightly damped and need 100 sec (1 min and 40 sec) or more, thus the lateral motion require a control to increase damping to get more suitable response.









The graph shows Root locus for the Dutch roll damper for τ of the washout circuit equal to 1 sec, its can be cleary seen that's is stable.

The graph shows Response of the aircraft (r) with Dutch roll damping for $S_{(yrg)} = 1.04$ volt/(deg/sec) for a pulse aileron deflection it can be clearly seen that response its clearly damped .		2				
The graph shows Response of the aircraft (δ_r) with Dutch roll damping for $S_{(yrg)} = 1.04$ volt/(deg/sec) for a pulse aileron deflection, it can be seen that the response of rudder deflection has small steady state error and satisfactory transit response.	x effect 0 5 4 3 2 1 2 1 2 3 4 3 4 3 4 5 0 4 5 0 1 2 3 4 5 0 1 2 3 4 5 0 1 2 3 2 3 4 5 0 1 2 3 2 3 4 5 0 1 2 3 3 3 3 3 3	2				



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6 Chapter Six: Conclusion

By the end of this project a lot of skills have been earned and important knowledge acquired. The overlapping between the control, dynamic and programming makes it deserves to spend the time on it to apply and manage the engineering work.

6.1 Conclusion

Synthesize of Design of Boeing747-E is studied and nonlinear nature of its lateral autopilot is focus on.

Although the designer had covered a big deal of work to overcome the problem occurred in lateral autopilot but still some weakness which we tried to overcome by using PD controller is proposed to damp the longitudinal oscillatory better than the one which is used, and a bure gain controller to enhance the Dutch roll oscillatory controller.

Results and comparison are carried out on chapters four and five, shows the difference between the proposed controller and the existing one which shows a better performance

6.2 Recommendations

Due to lack of data it was not easy to work with lateral motion, that we recommend and advice to work as a structural group projects, that can give a chance to design SUST aircraft and use its specifications to apply the theories. Some suggestions for a future work based on the results from the project are in the next section.

6.3 Future Work

As future work we suggest to make an autopilot for Boieng747-E by using another controlling technique and we suggest to work with fuzzy controller as future work and compare its results in longitudinal and lateral motion and the performance of the aircraft with the results of this project which (which is used PID controller not control tool box for SIMULINK).

we faced trouble effort while calculate all aerodynamic and stability derivative for the aircraft, thus we suggest to make program (may in Matlab) to calculate those derivative for every aircraft we inter it in the program.

References

1. Siddharth Goya., *Study of a Longitudinal Autopilot For Different Aircraft*.

2. Nelson, R.C., *Flight stability and automatic control. Vol. 2. 1998: WCB/McGraw Hill.*

3. BANDU. N. PAMAD, Performance, Stability, Dynamics, and Control of Airplanes.

4. Cook, M.V., Flight dynamics principles: a linear systems approach to aircraft stability and control. 2012: Butterworth-Heinemann.

5. JOHN H.BLAKELOCK., Automatic Control Of Aircaft and Missile

6. Mustafa Can Buken., FUZZY CONTROLLER DESIGN FOR LATERAL MOVEMENT FOR BOEING 747 AIRCRAFT.

7. Gloria Cortés Concha., Development of an Automatic Flight Control System .

Appendices

Appendix A

General parameters of Boeing 747-E:

Wing area (m^2)	510				
Aspect ratio	7.0				
Chord, \overline{c} (m)	8.3				
Total related thrust (KN)	900				
Centre of gravity (c.g.)	0.25 c				
Pilot's location (m)- relative to c.g.					
I _{xp}	26.2				
Izp	-3.05				
Weight (Kg)	250000				
Inertias (Kg m^2)					
I _{xx}	18.6× 10 ⁶				
I _{yy}	41.35× 10 ⁶				
I _{zz}	58× 10 ⁶				
I _{xz}	1.2×10^{64}				

Stability Characteristics of the Boeing 747-E:

1) Longitudinal Stability Characteristics:

Condition	2	5	7	9	10
h (ft)	SL	20,000	20,000	40,000	40,000
\mathbf{M}_{∞}	0.25	0.500	0.800	0.800	0.900
α (degrees)	5.70	6.80	0.0	4.60	2.40
W (lbf)	564,032.	636,636.	636,636.	636, 636.	636,636.
I_y (slug-ft ²)	$32.3 imes 10^6$	$33.1 imes 10^6$	$33.1 imes 10^6$	$33.1 imes 10^6$	$33.1 imes 10^6$
\mathbf{C}_L	1.11	0.680	0.266	0.660	0.521
\mathbf{C}_D	0.102	0.0393	0.0174	0.0415	0.0415
$\mathbf{C}_{L_{lpha}}$	5.70	4.67	4.24	4.92	5.57
$\mathbf{C}_{D\alpha}$	0.66	0.366	0.084	0.425	0.527
$\mathbf{C}_{m_{\alpha}}$	-1.26	-1.146	629	-1.033	-1.613
$\mathbf{C}_{L_{\dot{lpha}}}$	6.7	6.53	5.99	5.91	5.53
$\mathbf{C}_{m_{\dot{lpha}}}$	-3.2	-3.35	-5.40	-6.41	-8.82
$\mathbf{C}_{L_{q}}$	5.40	5.13	5.01	6.00	6.94
\mathbf{C}_{m_q}	-20.8	-20.7	-20.5	-24.0	-25.1
$\mathbf{C}_{L_{\mathbf{M}}}$	0.0	0875	0.105	0.205	278
$\mathbf{C}_{D_{\mathbf{M}}}$	0.0	0.0	0.008	0.0275	0.242
$\mathbf{C}_{m_{\mathbf{M}}}$	0.0	0.121	116	0.166	114
$\mathbf{C}_{L_{\delta_e}}$	0.338	0.356	0.270	0.367	0.300
$\mathbf{C}_{m_{\delta_e}}$	-1.34	-1.43	-1.06	-1.45	-1.20

- -

2) Lateral/Directional Stability Characteristics:

Condition	2	5	7	9	10
h (ft)	SL	20,000	20,000	40,000	40,000
\mathbf{M}_{∞}	0.25	0.500	0.800	0.800	0.900
α (degrees)	5.70	6.80	0.0	4.60	2.40
W (lbf)	564,032.	636, 636.	$636,\!636.$	$636,\!636.$	$636,\!636.$
I_x (slug-ft ²)	$14.3 imes 10^6$	18.4×10^6	18.2×10^{6}	18.2×10^{6}	$18.2 imes 10^6$
I_z (slug-ft ²)	$45.3 imes10^6$	$49.5 imes 10^6$	$49.7 imes 10^6$	$49.7 imes 10^6$	$49.7 imes 10^6$
I_{xz} (slug-ft ²)	-2.23×10^6	-2.76×10^6	0.97×10^6	-1.56×10^6	$35 imes 10^6$
$\mathbf{C}_{y_{eta}}$	96	90	81	88	92
$\mathbf{C}_{l_{eta}}$	221	193	164	277	095
$\mathbf{C}_{n_{\beta}}$	0.150	0.147	0.179	0.195	0.207
\mathbf{C}_{l_p}	45	323	315	334	296
\mathbf{C}_{n_p}	121	0687	0.0028	0415	0.0230
\mathbf{C}_{l_r}	0.101	0.212	0.0979	0.300	0.193
\mathbf{C}_{n_r}	30	278	265	327	333
$\mathbf{C}_{l_{\delta_{\alpha}}}$	0.0461	0.0129	0.0120	0.0137	0.0139
$\mathbf{C}_{n_{\delta_{\alpha}}}$	0.0064	0.0015	0.0008	0.0002	0027
$\mathbf{C}_{y_{\delta_r}}$	0.175	0.1448	0.0841	0.1157	0.0620
$\mathbf{C}_{l_{\delta_r}}$	0.007	0.0039	0.0090	0.0070	0.0052
$\mathbf{C}_{n_{\delta_r}}$	109	1081	0988	1256	0914

Appendix B

MATLAB Program

- 1) Longitudinal MATLAB Program
- a) Longitudinal MATLAB Program for Boeing 747-E Before Controller

```
%Being 747-E
%geometric data (will be added later)
%aerodynamic data (will be added later)
%nondimensional stability derivatives(latter)
%flight condition
g0=9.81;
theta0=0.0;
v0=158;
alpha=6.8*pi/180;
u0=v0*cos(alpha) ;
%dimensional longitudinal stability Derivatives
xu=-0.003;
xw=0.078;
zu=-0.07;
zw=-0.433;
zwd=-0.0157;
zz=1-zwd;
zq=-1.95;
mu=0.00008;
mw=-0.006;
mwd=-0.0004;
mq = -0.421;
8_____
xde=0.616;
zde=-5.15; %check
mde=-1.09;
8-----
a=[ xu xw
                    0
                            -q0*cos(theta0)
    zu/zz zw/zz (u0+zq)/zz -g0*sin(theta0)/zz
    mu+mwd*zu/zz mw+mwd*zw/zz mq+(u0+zq)*mwd/zz -mwd*g0*sin(theta0)/zz
       0 0 1 0]
b=[xde;zde/zz;mde+mwd*zde/zz;0.0];
%out put is pithch
c = [0 \ 0 \ 0 \ 1];
d=[0];
% transfer function representation
[num,den]=ss2tf(a,b,c,d)
printsys(num, den)
% check stability
r=roots(den)
for n=1:length(r)
    if real(r(n))<0.0</pre>
        disp('airplane is stable')
    else
        disp('airplane is not stable')
    end
end
    subplot(2,1,1)
% plot root locus
    rlocus(num, den)
 % short mode and phugoid roots
imagr1=imag(r(1))
```

```
imagr2=imag(r(2))
imagr3=imag(r(3))
imagr4=imag(r(4))
 for m=1:4
 if imagr1>imagr3
     disp('short period mode roots are')
     rsl=r(m)
     rs2=r(m)
     ns=real(r(m))
     ws=imag(r(m))
 end
 if imagr3<imagr1</pre>
     disp('phugoid mode roots are')
     rp1=r(m)
     rp2=r(m)
     np=real(r(m))
     wp=imag(r(m))
 end
 end
subplot(2,1,2)
%for input elevator deflection angle 0.2 rad
step(a, 0.2*b, c, d)
xlabel('time ')
ylabel('pitch angle (rad)')
```

b) Longitudinal MATLAB Program for Boeing 747-E After Controller

```
syms t;
t=0:0.1:100;
num=[-5 -6.255 -2.853];
den=[1 0.99 1.226];
i=tf(num,den);
num1=[-10];
den1=[1 10];
p=tf(num1,den1);
c=series(i,p);
num3=[1];
den3=[1 0];
s=tf(num3,den3);
a=series(c,s);
d=feedback(a,1);
subplot(2,1,1)
rlocus(d)
[a,b,c,d]=tf2ss(num,den)
printsys(a,b,c,d)
subplot(2,1,2)
%for input elevator deflection angle 0.2 rad
step(a, 0.2*b, c, d)
xlabel('time ')
ylabel('pitch angle (rad)')
```

- 2) Lateral MATLAB Program
- a) Lateral MATLAB Program for Boeing 747-E Before Controller

```
%Boeing 747-E
%geometric data (will be added later)
%aerodynamic data (will be added later)
%nondimensional stability derivatives(latter)
%flight condition
g0=9.81;
theta0=0.0;
v0=158;
alpha=0.0*pi/180;
u0=v0*cos(alpha) ;
%dimensional lateral stability Derivatives
yv=-0.1007;
yp=-0.281;
yr=0.443;
lv=-0.0176;
lp=-0.8766;
lr=0.5754;
nv=0.00497;
np=-0.0694;
nr=-0.281;
ix=-0.0645;
iz=-0.0207;
%control stability derivatives
vdr=4.1569;
yda=0.0;
ldr=0.0559;
lda=0.1852;
ndr=-0.5767;
nda=0.0080025;
xz=1-ix*iz;
8-----
%a=[yv yp g0*cos(theta0)
                                yr-u0
% (lv+ix*nv)/xz (lp+ix*np)/xz 0 (lr+ix*nr)/xz
 % (nv+iz*lv)/xz (np+iz*lp)/xz 0 (nr+iz*lr)/xz
  % nv np 0 nr]
a=[yv yp g0*cos(theta0) yr-u0
  lv lp 0 lr
  0 1 0 0
  nv np 0 nr]
b=[ydr 0
  (ldr+ix*ndr)/xz (lda+ix*nda)/xz
  0 0
  (ndr+iz*ldr)/xz (nda+iz*lda)/xz]
%out put is
c=[1 \ 0 \ 0 \ 0];
d = [1 \ 0];
% transfer function representation
%[num,den]=ss2tf(a,b,c,d)
%printsys(num, den)
% check stability
%r=roots(den)
%if you use ss
```

```
r=eig(a)
for n=1:length(r)
    if real(r(n))<0.0
        disp('airplane is stable')
    else
        disp('airplane is not stable')
    end
end
%for input elevator deflection angle 0.2 rad
t=0:0.1:100
step(a,0.2*b,c,d,1,t)
xlabel('time ')
ylabel('v (m/s)')</pre>
```

b) Lateral MATLAB Program for Dutch roll damper of Boeing 747-E After Controller

```
syms t;
t=0:0.1:100;
num=[-0.577 -0.0519 -0.0923];
den=[0.1814 0.98614 0.0191 0];
i=tf(num,den);
num1=[4];
den1=[1 4];
p=tf(num1,den1);
c=series(i,p);
s=1.04;
m=-1.6;
e=s*m;
d=feedback(c,e);
rlocus(d)
```