

## CHAPTER 6

### Design

#### 6.1. Distillation design:

##### 6.1.1. Introduction:

Distillation is most common class of separation processes and properly of the better-understand unit operation that uses the difference in relative volatilities , or differences in boiling of the component to be separated, it is the most widely used method of separation in the process industries

##### -Types of distillation column:

- 1- Single flash vaporization.
- 2- Packed towers.
- 3- Plates towers.
  - a) Bubble cap towers.
  - b) Sieve pates.
  - c) Valve plates towers.

**-Sieve trays:** Sieve trays offer several advantage over bubble-cap trays , and their simpler and cheaper construction has led to their increasing use . the general form of the flow on a sieve tray is typical of a cross flow system with perforation in the tray taking the place of the more complex bubble caps . the key differences in operation between these two types of tray should be noted . with the sieve tray the vapor passes vertically through the holes into the liquid on the tray , where as with the bubble cap the vapor issues in an approximately horizontal direction from the slots . with the sieve plate the vapor velocity through the perforation must be greater than a certain minimum value in order to prevent the weeping of the liquid stream down through the holes . at the other extreme , a very high vapor velocity leads to excessive entrainment and loss off tray efficiency .

##### 6.1.2. Collect the data of fluid to be distillated and distillated fluids:

##### -Feed stream:

At 403<sup>0</sup> K, 2000 KPa.

Table (6.1) feed stream composition.

Component	Mole flow (kmol/h)	Mole%	Mass flow (kg/h)	Wt%
methanol	2516.10	0.217006616	80615.844	0.125340067
isobutylene	428.05	0.036918138	24017.8855	0.037342577
1-butene	1817.511622	0.156755275	101977.3431	0.158552542
2-butene	5172.917692	0.44614963	290236.8929	0.451255111
MTBE	1660.00	0.14317034	146329	0.227509702
water	0	0	0	0
<b>Total</b>	<b>11594.58</b>	<b>1</b>	<b>643176.9655</b>	<b>1</b>

**-Top product stream :**

At 400 ° K, 1900KPa.

Table (6.2) top stream composition

Component	Mole flow (kmol/h)	Mole%	Mass flow (kg/h)	Wt%
methanol	2428.7308	0.246641613	77816.57994	0.157508615
isobutylene	428.0505	0.0434689	24017.914	0.0486161
1-butene	1817.512	0.1845792	101975.46	0.2064048
2-butene	5172.912	0.5253107	290236.83	0.5874676
MTBEs	0	0	0	0
water	0	0	0	0
<b>Total</b>	<b>9847.236</b>	<b>1</b>	<b>494046.06</b>	<b>1</b>

**-Bottom product stream:**

At 440 ° K, 1925.175 KPa

Table (6.3) bottom stream composition

Component	Mole flow (kmol/h)	Mole%	Mass flow (kg/h)	Wt%
methanol	87.36842105	0.05	2799.284211	0.018770981
isobutylene	0	0	0	0
1-butene	0	0	0	0
2-butene	0	0	0	0
MTBE	1660	0.95	146329	0.981229019
water	0	0	0	0
<b>Total</b>	<b>1747.368421</b>	<b>1</b>	<b>149128.2842</b>	<b>1</b>

**-Relative volatility:**

Table (6.4) average relative volatility of composition.

Component	$\alpha_{\text{feed}}$	$\alpha_{\text{top}}$	$\alpha_{\text{bottom}}$	Aav
methanol	1.186110097	1.162297499	1.448866438	1.265758
isobutylene	4.214615978	4.270349142	3.743897719	4.076288
1-butene	4.281515808	4.345063797	3.73236071	4.119647
2-butene	3.479708054	3.515657126	3.194453855	3.396606
MTBE	1	1	1	1
water	0.381770611	0.369823631	0.51937441	0.423656

**6.1.3. Heavy and light key:**

Heavy key: mtbe

Light key: methanol.

**6.1.4. Type of tray:**

Sieve tray.

**6.1.5. Determination of minimum reflux ratio:**

$$\sum \frac{\alpha x}{\alpha - \emptyset} = R_m + 1 \quad \longrightarrow \quad (1)$$

$\alpha$  = average Relative volatility of any component.

X = mole fraction of component in Distillate.

$\emptyset$  = Constant.

$R_m$  = Minimum reflux ratio.

$$\sum \frac{\alpha z_f}{\alpha - \emptyset} = 1 - q \quad \longrightarrow \quad (2)$$

Where:

$Z_f$  = mole fraction of component in feed stream.

q = feed quality

$$q = \frac{HG - HF}{HG - HL}$$

Where:

HG = Enthalpy of gas at the feed dew point (KJ/Kmol)

HL=Enthalpy of liquid at the feed bubble point (KJ/Kmol)

HF=Enthalpy of feed at 403° K.

$$q = \frac{1.91827 - 1.4672}{1.91827 - 1.67614} = 1.86$$

Substitute in equation (2) to find( $\emptyset$ )

$$\sum \frac{\alpha z^f}{\alpha - \emptyset} = 1 - 1.86$$

$$\sum \frac{\alpha z^f}{\alpha - \emptyset} = -.86$$

$$\frac{1.265758 \times 0.217007}{1.265758 - \emptyset} + \frac{4.076288 \times 0.036918}{4.076288 - \emptyset} + \frac{4.119647 \times 0.156755}{4.119647 - \emptyset} + \frac{3.396606 \times 0.44615}{3.396606 - \emptyset} + \frac{1 \times 0.14317}{1 - \emptyset} + \frac{.423656 \times 0}{.423656 - \emptyset} = 0$$

Solving  $\emptyset$  By try & error:

$$\emptyset = 1.047365$$

Substitute in equation (1) to find Rm:

$$\frac{1.265758 \times 2.46641613}{1.265758 - \emptyset} + \frac{4.076288 \times 0.043469189}{4.076288 - \emptyset} + \frac{4.119647 \times 0.184571192}{4.119647 - \emptyset} + \frac{3.396606 \times 0.525318007}{3.396606 - \emptyset} + \frac{1 \times 0}{1 - \emptyset} + \frac{.423656 \times 0}{.423656 - \emptyset} = R_m + 1$$

$$R_m = 1.494995$$

### 6.1.6. Calculation of the actual ratio(R)

The rule of thumb is:

$$R = (1.2 \text{ ----- } 1.5) R_{\min}$$

$$R = 1.2 R_m$$

$$= 1.2 \times 1.5 = 1.8$$

### 6.1.7. Calculation of the minimum number of theoretical stages:

$$N_{\min} = \frac{\ln \left( \frac{X_{lk}}{X_{hk}} \right)_D \times \left( \frac{X_{hk}}{X_{lk}} \right)_B}{\ln \alpha_{lk}}$$

Where:

$X_{lk}$ =mole fraction of light key.

$X_{hk}$ = mole fraction of heavy key.

$\alpha_{lk}$ = average relative volatility of light key.

$N_{\min}$ = 26 stages

**6.1.8. Calculation of the number of theoretical stages:**

$$N - N_{\min} / N + 1 = 0.75 \left[ 1 - \left( R - R_{\min} / R + 1 \right)^{0.566} \right]$$

$$\frac{R - R_{\min}}{R + 1} = \frac{1.8 - 1.5}{1.8 + 1} = 0.1$$

From Gilland relation.

$$\frac{N - N_{\min}}{N + 1} = 0.54$$

$$N = 57.695 \text{ stages}$$

**6.1.9. Calculation of the column efficiency ( $E_o$ ):**

$$E_o = 0.5278 - 0.27511 \log(\alpha k^* \mu F) + 0.04493 (\log(\alpha k^* \mu F))^2$$

$$\mu F = 0.2161$$

$$E_o = 69.29\%$$

**6.1.10. Calculation of the number of actual stages ( $N_a$ ):**

$$N_a = \frac{N}{E_o} \\ = \frac{57.695}{0.6929} = 83.265 \text{ stages}$$

**6.1.11. Calculation of the height of the column ( $H_t$ ):**

$$H_t = N \times C + \frac{(N-1) \times c}{10} + 0.2 \times H_t$$

C: tray spacing = 0.609 (so as to ensure accessibility for cleaning)

$$0.8 H_t = 84 \times 0.3 + \frac{(84-1) \times 0.3}{10} = 27.69$$

$$H_t = 34.6 \text{ m .}$$

**6.1.12. Determination of the feed plate location (m):**

$$\frac{n}{m} = \left[ \left( \frac{z h k}{z l k} \right)_f \times \left( \frac{x l k}{x h k} \right)_D^2 \times \frac{B}{D} \right]^{0.206}$$

$$D = 9847.2118 \text{ kmol/h} \quad B = 1747.368 \text{ kmol/h}$$

$$\frac{n}{m} = \left[ \left( \frac{0.14317034}{0.217006616} \right)_f \times \left( \frac{0.2396416}{0.007} \right)_D^2 \times \frac{1747.368}{9847.2118} \right]^{0.206} = 2.7561$$

$$m = \frac{N}{1 + \frac{n}{m}} = \frac{84}{1 + 2.7561} = 22.36 \text{ stages} \approx 22$$

$$m = 22 \text{ stage}$$

the feed enter the column at tray no 22 from the Bottom.

### 6.1.13. Calculation of the tower diameter(D):

The following areas terms are used in the plate design procedure:

$A_t$ =Total column cross- sectional area,

$A_d$ =cross-sectional area of down comer,

$A_n$ =Net area available for vapor-liquid disengagement , normally equal to  $A_c - A_d$  for asingle pass plate,

$A_a$ = Active or bubbling , area, equal to  $A_c - 2A_d$  for single- pass plates,

$A_o$ =Hole area, the total area of all the active holes,

$A_p$ = perforated area (including blanked areas),

$A_{ap}$ = The clearance area under the down comer apron.

#### -Top diameter calculation:

$$U_F = K \sqrt{\frac{\rho_L - \rho_V}{\rho_V}}$$

Where:

$U_F$ = flooding vapor velocity (m/s) based on the net column cross sectional area  $A_n$ .

$K$ =constant obtained from figure(1)appendix (A)

$$F_{LV} = \frac{\bar{L}}{\bar{V}} \sqrt{\frac{\rho_V}{\rho_L}}$$

Where:

$F_{LV}$ =The vapor liquid flow factor in figer (1) appendix

$\bar{L}$  = Liquid mass flow rate kg/s

$\bar{V}$  =Vapor mass flow rate kg/s

Top Diameter calculations:

$$\frac{\bar{L}}{\bar{V}} = \frac{R}{R + 1} = \frac{1.8}{1.8 + 1} = 0.64$$

From ideal gas law:

$$PV = nRT$$

$$\rho_V = \frac{T_o P M_{wt}}{T P_o V_o} = \frac{273.5 \times 19 \times 50.17}{400 \times 1 \times 22.4} = 29.09 \text{ Kg/m}^3$$

$$F_{LV} = 0.64 \sqrt{\frac{29.09}{467.37}} = 0.160$$

From figuer (1) appendix (A)

$$K=0.05$$

$$U_F = 0.05 \times \sqrt{\frac{467.37 - 29.09}{29.09}} = 0.753$$

Design velocity (U) = 80% of ( $U_F$ )

$$U = 0.8 \times 0.753 = 0.602 \text{ m/s}$$

$$A_n = \frac{V_1}{\rho v \times U \times 3600} = \frac{(1+R)D}{\rho v \times U \times 3600} = \frac{(1+1.8) \times 9847.2118}{29.09 \times 0.602 \times 3600} = 0.437 \text{ m}^2$$

$$A_d = 0.12 A_t$$

$$A_n = A_t - 0.12 A_t = 0.88 A_t$$

$$A_t = \frac{A_n}{0.88} = \frac{0.437}{0.88} = 0.496 \text{ m}^2$$

$$D = \left( \frac{4A_t}{\pi} \right)^{0.5} = 0.79 \text{ m}$$

**-Bottom diameter calculations:**

$$\bar{L} = (q \times F) + L$$

From Ideal gas law:

$$PV = nRT$$

$$\rho v = \frac{T_o P M_{wt}}{T P_o V_o} = \frac{273.15 \times 19.252 \times 85.34}{440 \times 1 \times 22.4} = 45.53$$

$$F_{LV} = 1.046 \sqrt{\frac{45.53}{728.228}} = 0.261$$

From figure (1) appendix (A) at FLV = 0.261 and spacing 60 mm

$$K=0.046$$

$$U_F = 0.046 \times \sqrt{\frac{728.228 - 45.53}{45.53}} = 0.178 \text{ m/s}$$

Design velocity (U) = 80% of flooding velocity ( $U_F$ )

$$0.8 \times 0.178 = 0.1424 \text{ m/s}$$

$$A_n = \frac{V}{\rho v \times U \times 3600} = \frac{27572.19}{45.53 \times 0.1424 \times 3600} = 1.198 \text{ m}^2$$

Down comer area = 12% from total area =  $0.88 A_t$

$$A_t = \frac{A_n}{0.88} = \frac{1.198}{.88} = 1.36 \text{ m}^2$$

$$D = \left( \frac{4A_t}{\pi} \right)^{0.5} = \left( \frac{4 \times 1.36}{3.14} \right)^{0.5} = 1.3172 \text{ m.}$$

Taking the bottom diameter for the entire tower since it is the greatest diameter.

$$A_t = 1.36 \text{ m}^2$$

$$A_d = 0.12 A_t$$

$$= 0.12 \times 1.36 = 0.1632 \text{ m}^2$$

$$A_a = A_t - 2A_d$$

$$= 1.36 - 2(0.1632) = 1.0336m^2.$$

$$A_o = 0.1 \times A_a = 0.10336m^2.$$

$$A_c = 0.07 \times A_t = 0.07 \times 1.36 = 0.0952m^2.$$

**- $A_p$ =Preformatted area:**

When down comer area =  $0.12 \times A_t$

$$\frac{LW}{D} = 0.75 \text{ (From figure (4) appendix (A)) } \& \theta_c = 98^\circ \text{ (from figure(5) appendix (A))}$$

Where  $L_W$  : Weir length.

$$L_W = 0.75 \times D = 0.75 \times 1.3172 = 0.9879 \text{ M}$$

Angle subtended at plate edge by imperforated strip =  $180 - 98 = 82^\circ$

Calming zones width = 50mm

Mean Length, imperforated edge strips

$$= (1.3172 - 50 \times 10^{-3}) \pi \times \left( \frac{82}{180} \right) = 1.813 \text{ m.}$$

Area of imperforated edge strips =  $50 * 10^{-3} \times 1.813 = 0.0906 m^2$ .

Mean length of calming zone =  $(1.3172 - 50 * 10^{-3}) \sin\left(\frac{98}{2}\right) = 0.9563m$

Area of calming zone =  $2(0.9563 * 50 * 10^{-3}) = 0.09563m^2$

Total area for perforations,  $A_p = 1.336 - 0.0906 - 0.09563 = 0.8473m^2$

$$\frac{A_o}{A_p} = 0.1 \left( \frac{A_a}{A_p} \right) = 0.1 \left( \frac{1.0336}{0.8473} \right) = 0.12198.$$

$$\frac{A_o}{A_p} = 0.9 \left( \frac{d_o}{L_p} \right)^2$$

Where  $L_p$  : hole pitch.

$$0.12198 = 0.9 \left( \frac{d_o}{L_p} \right)^2$$

$$\left( \frac{d_o}{L_p} \right)^2 = 0.1355$$

$$\left( \frac{L_p}{d_o} \right) = 2.716.$$

2.716 are satisfactory, within 2.5 to 4.0.

### 6.1.14. Determination of fractional entrainment ( $\phi$ ):

From figure (2) appendix (A)

At  $F_{LV}=0.261$  and 80% flooding  $\phi=0.09$ (well below 0.1).

$$e = \frac{\phi \times L}{1 - \phi} = \frac{0.009 \times 17724.98}{1 - 0.009} = 160.973 \text{ kg/h.}$$

### 6.1.15. Weeping point:

Weeping will occur when  $U_o(\text{min}) < U_o(\text{min})$  calculated.

$$U_o = \frac{V}{\rho V \times A_o} = \frac{37543.53194}{45.53 \times 0.10336 \times 3600} = 2.3175 \text{ m/s}$$

Taking 70% turn down.

$$U_o(\text{min}) = 0.7 \times U_o = 0.7 \times 2.3175 = 1.624 \text{ m/s.}$$

$$U_o(\text{min}) \text{ calculated} = \frac{k_2 - 0.9(25.4 - d_o)}{\rho_v^{0.5}}$$

$$d_o = 5 \text{ mm}$$

$k_2$  is a function of  $(h_w + h_{ow}(\text{min}))$

$h_w$ : weir height = 23 mm

$$h_{ow}(\text{min}): \text{minimum weir crest} = 750 \times \left( \frac{L_{min}}{\rho_l L_w} \right)^{2/3}$$

$$L_{min} = 0.7 \times 17724.98 = 12407.486 \text{ kg/h.}$$

$$h_{ow}(\text{min}) = 750 \times \left( \frac{12407.486}{728.228 \times 0.9879 \times 3600} \right)^{2/3} = 21.31$$

$$h_w + h_{ow}(\text{min}) = 23 + 21.31 = 44.31 \text{ mm.}$$

From figure (3) appendix (A)

$$k_2 = 30$$

$$U_o(\text{min}) \text{ calculated} = \frac{30 - 0.9(25.4 - 5)}{(45.53)^{0.5}} = 1.5 \text{ m/s.}$$

$\therefore$  Weeping will not occur.

### 6.1.16. Pressure drop calculation:

$$\Delta P = 9.81 \times h_t \times 10^{-3} \times \rho_l$$

$$h_t = h_d + (h_w + h_{ow}) + h_r$$

$$h_d = 51 \left( \frac{U_o}{C_o} \right)^2 \frac{\rho_v}{\rho_l}$$

From figure (6) appendix (A)

$$\text{At } \frac{A_o}{A_p} = 12.198\% \& \frac{\text{plate thickness}}{\text{hole thickness}} = 1$$

$$C_o=0.859$$

$$h_d = 51 \left( \frac{2.3175}{0.859} \right)^2 \frac{45.53}{728.228} = 23.208 \text{ mm.}$$

$$h_{ow}(\text{min}) = 750 \times \left( \frac{27503.63}{728.228 \times 0.9879 \times 3600} \right)^{2/3} = 36.23 \text{ mm.}$$

$$h_w = 23 \text{ mm}$$

$$h_r = \frac{12.5 \times 10^3}{\rho_l} = \frac{12.5 \times 10^3}{728.228} = 17.16$$

$$h_t = 21.31 + 36.23 + 23 + 17.16 = 97.7 \text{ mm}$$

$$\Delta P = 9.81 \times 97.7 \times 10^{-3} \times 728.228 = 0.007 \text{ bar/tray.}$$

### 6.1.17. Down comer liquid back up:

For safe design and to avoid flooding

$$h_b < \frac{1}{2}(C + h_w)$$

$$h_b = h_t + h_d + h_w + h_{ow} + h_r + h_{dc}$$

$$h_{dc} = 166 \left( \frac{L}{\rho_l A_{ap}} \right)^2$$

$$A_{ap} = h_{ap} \times L_w$$

$$h_{ap} = h_w - 10 \text{ mm}$$

$$23 - 10 = 13 \text{ mm}$$

$$A_{ap} = 0.9879 \times 10^{-3} \times 13 = 0.013 \text{ mm}$$

$$h_{dc} = 166 \left( \frac{17724.98}{728.228 \times 0.013 \times 3600} \right)^2 = 4.64 \text{ mm}$$

$$h_b = 97.7 + 36.23 + 23 + 4.67 = 201.83 \text{ mm}$$

$$\frac{1}{2}(C + h_w) = \frac{1}{2}(0.3 + 23 \times 10^{-3}) = 0.323 \text{ m.}$$

$$h_b < \frac{1}{2}(C + h_w) \text{ no flooding will occur.}$$

### 6.1.18. Down comer residence time:

$$t_r = \frac{A_d h_b \rho_l}{L}$$

$$= \frac{0.1632 \times 0.2018 \times 728.228}{(17724.98/3600)} = 4.8 \text{ sec.}$$

4.8 > 3 so it is acceptable.

### 6.1.19. Thickness calculation:

- column thickness:

Highest operating temperature is  $166.85^{\circ}\text{C}$ .

Design stress at  $166.85^{\circ}\text{C} = 111 \text{ N/mm}^2$ .

Joint efficiency = 0.85.

$$e = \frac{P_i D_i}{2Jf - P_i}$$

$$= \frac{1925175 \times 1.3172}{2 \times 111 \times 10^6 \times 0.85 - 1925175} = 0.01357 \text{ mm.}$$

Corrosion allowance 2mm.

$\therefore$  column thickness = 2.01357mm.

**-Head thickness:**

- Ellipsoidal heads:

$$e = \frac{P_i D_i}{2Jf - 0.2P_i}$$

$$= \frac{1925175 \times 1.3172}{2 \times 111 \times 10^6 \times 0.85 - 1925175} = 0.011 \text{ m.}$$

-Tori spherical head

$$e = \frac{P_i C_s R_c}{2Jf - (C_s - 0.2)}$$

$C_s \equiv$  stress cocentration factor for torispherical head.

$$C_s = \frac{1}{4} (3 + \sqrt{R_c / R_k})$$

$R_c \equiv$  crown radius.

$$\frac{R_c}{R_k} = \text{no less than } 0.6.$$

$R_k \equiv$  knukle radius.

$$R_c \equiv D_i$$

$$R_k \equiv 0.6D_i.$$

$$C_s = \frac{1}{4} (3 + \sqrt{1/0.6}) = 1.072.$$

J=1(No joint in head).

$$E = \frac{1925175 \times 1.072 \times 1.3172}{2 \times 111 \times 10^6 + (1.072 - 0.2)} = 0.01224 \text{ mm.}$$

Ellipsoidal heads IS recommended since it has the smallest thickness

$\therefore$  head thickness = 0.011mm.

Table (6.5) summary of design calculation.

Parameter	Value
<b>Tower diameter</b>	1.3172M
<b>Tray spacing</b>	0.30
<b>Tower Height</b>	34.6M
<b>Total area(cross sectional area)</b>	1.36m <sup>2</sup>
<b>Down comer area</b>	0.1632m <sup>2</sup>
<b>Net area</b>	1.19m <sup>2</sup>
<b>Active area</b>	1.0336m <sup>2</sup>
<b>Hole area</b>	0.10336m <sup>2</sup>
<b>Number of theoretical stages</b>	57.695 stages
<b>Tower efficiency</b>	69.29%
<b>Plate thickness</b>	0.005M
<b>Weir height</b>	0.005M
<b>Weir length</b>	0.987M
<b>Hole diameter</b>	0.005M
<b>Fractional entrainment</b>	0.09
<b>Weeping velocity</b>	1.5M/S
<b>Total presser drop head</b>	0.007 bar
<b>thickness Of column</b>	2.01357MM
<b>thickness Of head</b>	0.011MM

## 6.2. Reactor design:

### -Type of reactor proposed:

A packed bed reactor, which is essentially a plug flow reactor packed of solid catalyst particles to speed up the reaction.

### -Justification of selection:

- Adiabatic packed bed reactor, is the cheapest type of reactors and simple to design and construction.
- It give the highest conversion per weight of catalyst of any catalyst reactor.
- Running the reactor adiabatically allows to recover heat from the high temperature product and reduce cost of energy.

“The process uses an acidic ion-exchange-resin catalyst.”

### 6.2.1. Design calculation:



Conversion: 80% of isobutylene.

#### -Input and output stream:

Table (6.6) Summary of material balance around reactor.

Component	Input(Kmol/h)	Output(Kmol/h)
Methanol	4176.10	2516.10
Isobutylene	2088.05	428.05
1-butene	1817.511622	1817.511622
2-butene	5172.917692	5172.917692
Mtbe	0.00	1660.00
water	0.00	0.00
Total	13254.58	11594.58

#### -Rate law:

$$-r_A = k_f \frac{C_{\text{isobutylene}}}{C_{\text{methanol}}} - k_r \frac{C_{\text{mtbe}}}{C_{\text{methanol}}^2}$$

Where:

$$k_r = 1.464 \times 10^{22} \exp\left(-\frac{129,600}{RT}\right)$$

$$k_f = 6.05 \times 10^{16} \exp\left(-\frac{85,400}{RT}\right)$$

$$C_{\text{isobutylene}} = C_{A_0}(1 - X_A)$$

$$C_{\text{methanol}} = C_{A_0}(\theta_{\text{meth}} - X_A)$$

$$C_{\text{mtbe}} = C_{A_0}(\theta_{\text{mtbe}} + X_A)$$

“The units of reaction rate,  $r_i$ , are mol/m<sup>3</sup>h, and the activation energy is in J/mol.”

Design equation:

$$\frac{dF_A}{dV} = F_{A_0} \left(\frac{dX_A}{dV}\right) = -r_A = k_f \frac{C_{\text{isobutylene}}}{C_{\text{methanol}}} - k_r \frac{C_{\text{mtbe}}}{C_{\text{methanol}}^2}$$

$$dV = \frac{F_{A0}}{k_f \frac{C_{\text{isobutylene}}}{C_{\text{methanol}}} - k_r \frac{C_{\text{mtbe}}}{C_{\text{methanol}}^2}} dX_A \quad \longrightarrow \quad (1)$$

$$\int_0^V dV = F_{A0} \int_0^{0.8} \frac{dX_A}{k_f \frac{C_{\text{isobutylene}}}{C_{\text{methanol}}} - k_r \frac{C_{\text{mtbe}}}{C_{\text{methanol}}^2}} \quad \longrightarrow \quad (2)$$

- Integration of right side of equation (2)

Since the reactor is adiabatic, temperature (T) and conversion(X) are related by the following equation:

$$X_A = \frac{\sum \theta_i C_{pi} (T - T_0)}{-\Delta H_{RX}}$$

Calculations were made by using Excel, and data need is constructed with the aid of equation (2), and tabulated in table (6.7):

Table (6.7) relation between conversion & temperature

T	X	F(x)
<b>358.0001</b>	0	0.095535
<b>362.5341</b>	0.091711	0.070099
<b>367.0681</b>	0.180646	0.05221
<b>371.6021</b>	0.26688	0.039508
<b>376.1361</b>	0.350477	0.030415
<b>380.6701</b>	4.31E-01	0.023869
<b>385.204</b>	5.10E-01	0.019149
<b>389.738</b>	0.586016	0.015773
<b>394.272</b>	0.659605	0.013431
<b>398.806</b>	0.730798	0.011961
<b>403.34</b>	0.79963	0.011381

These data are plotted in figure (6.1) below:

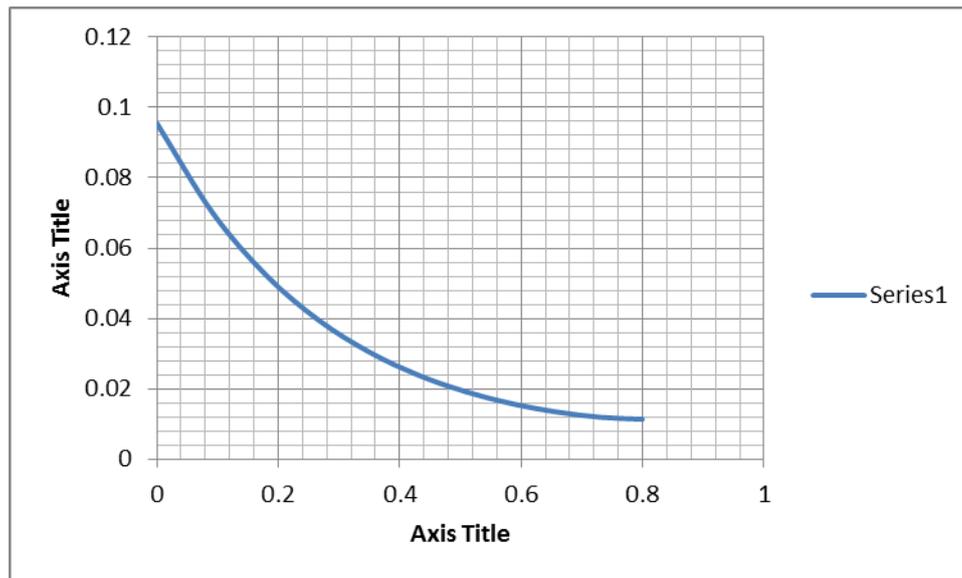


Figure (6.1) integration plot.

The area under the curve  $A = 0.031534679$

$$\therefore \frac{V}{F_{A_0}} = A$$

$$\rightarrow V = F_{A_0} \times A$$

$$V = 2088.05 \times 0.031534679 = 65 \text{ m}^3$$

$$V = \frac{\pi D^2 L}{4}$$

$$\text{Put } L = 13.8D$$

$$V = \frac{\pi D^2 \times 13.8D}{4}$$

$$\rightarrow D = \sqrt[3]{\frac{V}{10.8}} = \sqrt[3]{\frac{65}{10.8}} = 1.8 \text{ m.}$$

$$L = 13.8 \times 1.8 = 24.8 \text{ m.}$$

#### **-Reactor thickness:**

Highest operating temperature is  $403^\circ\text{K}$

Design stress at  $403^\circ\text{K} = 70 \text{ N/mm}^2$

$$e = \frac{P_i D_i}{2Jf - P_i}$$

$$\frac{1925175 \times 1.8}{2 \times 70 \times 10^6 \times 0.85 - 1925175} = 29.59$$

Corrosion allowance 2mm.

∴ Reactor thickness =31.59mm.