### **Dedication**

# To my parents, brothers, sisters and husband

## **Acknowledgement**

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#### **Abstract**

We show frames of the structure of Riesz bases, a method of sampling expansions on a semi-inner product and reproducing Kernel on Banach spaces with a norm. We also show that an integral formula for the duality between tensor products and homogenous polynomials on Banach spaces. James boundaries in dual Banach spaces are .considered

تم تو ضيح الا طارات وبناء اساس ريس وطريقة تفككات أخذ العينات في شبه الضرب الداخلي و نواة اعادة التوليدعلي فضاءات باناخ طبقاً للنظيم. ايضاً تم توضيح صيغة التكامل لأجل الثنائية بين ضرب المم تدات و كثيرات الحدود المتجانسه علي فضاءات باناخ. تم إعتبار الحديات في فضاءات باناخ الثنائيه.

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