# DeDication

To My father,

Mother,

Brothers,

**Sisters** 

and husband

# Acknowl edgements

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#### **Abstract**

We study the gluing problem widely met in the fusion systems of the symmetric and linear groups. We show the global regularity for sub-groups for sub-Laplace equations on homogenous groups and the structure of power bounded elements of locally compact groups. We give applications to group representations and functional equations.

### الخلاصة

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