# CHAPTER FIVE 

RESULTS AND
DISCUSSION

## Chapter five <br> Results and discussion

This chapter therefore considers the design of retaining wall structures, in particular the calculations and practical considerations necessary for the control of cracking.

All these aspects of design are outlined and illustrated with a detailed design example of a cantilever type retaining wall.

### 5.1 Laboratory Results:

Liquid Limit $=69$
Plastic Limit $=25.8$
Plasticity Index $=40$
Referring to table (3.1) Relation between Plasticity Index and Potential Swell this soil is high Potential Swell They found that using the method of removal and replacement by non-swelling soils significantly reduced the swelling characteristics.

### 5.2 Design Procedure:

STEP (1):
Determination of dimension of the tank
Quantity =per demand x Population
Every personal uses approximately 140-150 liters of water a day
Number of residents $=600$
Daily water requirement $=150 * 600=90000$ liter per day $=90 \mathrm{~m}^{3}$
Assuming length is equal to the three times of breadth.
Area of the $\operatorname{tank}=\frac{\mathrm{Q}}{\mathrm{H}}$
Assuming $\mathrm{H}=3 \mathrm{~m}$
Area of the $\operatorname{tank}=\frac{90}{3}=30 \mathrm{~m}^{2}$
$B=\sqrt{ }($ area of tank $/ 3)$
$B=\sqrt{ }(30 / 3)=3.16=\sim 3.20 \mathrm{~m}$
$\mathrm{L}=3 \mathrm{~B}, \mathrm{~L}=3 * 3.20=9.60 \mathrm{~m}$
Assuming Free board $=500 \mathrm{~mm}$
Density $\gamma=1800 \mathrm{~kg} / \mathrm{m} 3=17.6 \mathrm{kN} / \mathrm{m}^{3}$
Angle of internal friction $\phi=30^{\circ}$
Angle of internal friction of foundation soil $\phi=33^{\circ}$
The assumed surcharge load $=50 \mathrm{KN} / \mathrm{m}^{2}$
STEP (2):
Estimation of primary dimensions of the wall,
The dimensions of the retaining wall will be assumed as follow refer to
figure4.3
a. The width of the wall base
$\mathrm{B}=0.4 \mathrm{H}$ to $0.7 \mathrm{H}=0.4 * 4$ to $0.7 * 4$
$B=1.6 \mathrm{~m}$ to 2.569 m , the width of the base will be assumed $=3.20 \mathrm{~m}$
b. The thickness of the stem at the top
$\mathrm{t}=\mathrm{H} / 12$ to $\mathrm{H} / 10$
$\mathrm{t}=0.33$ to 0.4 m take $\mathrm{t}=0.4 \mathrm{~m}$

## Check of soil stresses

(In case of during maintenance)


Fig. 5.1 loads on the wall

## 1. The loads:

Calculate total weight including walls
$\mathrm{W}_{\text {wall } 1}=25^{*}(0.3 * 4)=27 \mathrm{KN}$
$\mathrm{W}_{\text {wall } 2}=25^{*}\left(0.5^{*} 0.1^{*} 3.6\right)=4.5 \mathrm{KN}$
$\mathrm{W}_{\text {floor }}=25^{*}\left(0.4^{*} 1.60\right)=16 \mathrm{KN}$
The sum of these weights ( N ):
$\mathrm{N}=27+4.5+16=47.50 \mathrm{KN}$
$\mathrm{M} @ 0=(27 * 0.55)+(4.5 * 0.434)+(16 * 0.8)=29.60 \mathrm{KN} . \mathrm{m}$
$\mathrm{A}=1.6 \mathrm{~m}^{2}$
$\mathrm{Z}=0.43 \mathrm{~m}^{3}$
$\mathrm{p}_{\max }=\frac{\sum 47.50}{1.6}+\frac{\sum 29.60}{0.43}$
$=98.52<$ (soil bearing capcity $=180$, unsafe $)$
$\mathrm{p}_{\min }=\frac{\sum 47.50}{1.6}-\frac{\sum 29.60}{0.43}=-39.15($ tension, unsafe $)$

## Use toe with length= 1.73 m

(In case of during maintenance)


Fig. 5.2 loads on wall with toe

The loads and earth pressures acting on the wall:
II. The loads:
$\mathrm{W}_{\text {wall } 1}=25 *(0.3 * 4)=27 \mathrm{KN}$
$\mathrm{W}_{\text {wall } 2}=25^{*}\left(0.5^{*} 0.1^{*} 3.6\right)=4.5 \mathrm{KN}$
$\mathrm{W}_{\text {floor }}=25^{*}(0.4 * 3.20)=32 \mathrm{KN}$
$\mathrm{W}_{\text {back fill }}=17.6^{*} 3.6^{*} 1.73=109.61 \mathrm{KN}$
$\mathrm{W}_{\text {surcharge }}=50 * 1.73=86.65 \mathrm{KN}$
The sum of these weights:
$\sum W=\sum R_{V}=\Sigma 259.76 \mathrm{KN}$

## 2. The active earth pressures:

$K_{a}=\frac{1-\sin \phi}{1+\sin \theta}=\frac{1-\sin 30}{1+\sin 30}=0.33$
The horizontal pressure at depth y from the top of the surcharge is:
$17.6 \mathrm{y} \frac{(1-0.5)}{(1+0.5)}=5.87 \mathrm{y} \mathrm{kN} / \mathrm{m}^{2}$
The horizontal pressure at the base is
$5.87 \times 4=23.48 \mathrm{kN} / \mathrm{m}^{2}$
(i) Maximum soil pressure the base properties are:
$\mathrm{R}_{\mathrm{V}}{ }^{*} \mathrm{x}=\mathrm{M}_{\mathrm{R}}-\mathrm{M}_{0}$
$\overline{\mathrm{X}}=\frac{\sum \mathrm{M}_{\mathrm{R}}-\sum \mathrm{M}_{0}}{\sum \mathrm{RV}}=\frac{548.81-193.44}{259.76}=1.37 \mathrm{~m}$
$e=\frac{b}{2}-\bar{x} \quad=1.28-1.37=0.23 \mathrm{~m}$


Fig. $\mathbf{5 . 3}$ the pressure distribution under the wall
$\bar{B}=B-2 e=3.2-2 * 0.23=2.74$
Area A=2.74 m ${ }^{2}$
The maximum soil pressure at a calculated for service load is:
$=\frac{259.76}{2.74}\left(1+\frac{6 * 0.23}{2.74}\right)=142.55 \mathrm{KN} / \mathrm{m}^{2}$
The minimum soil pressure at C calculated for service load is
$\frac{259.76}{2.74}\left(1-\frac{6 * 0.23}{2.74}\right)=44.55 \mathrm{kN} / \mathrm{m}^{2}$
$\partial_{1}=\mathrm{ka} * \mathrm{q}=.33 * 50=16.5$
$\mathrm{E}_{\mathrm{a} 1}=16.5 * 4=66 \mathrm{kN}$
$\partial_{2}=\mathrm{ka} *\left(\mathrm{q}+\mathrm{H}^{*} \gamma\right)=0.33 *\left(50+17.6^{*} 4\right)=39.73$
$\mathrm{E}_{\mathrm{a} 2}=0.5 *\left(\partial_{2}-\partial_{1}\right) * 4=46.2 \mathrm{KN}$
(ii) Stability against overturning: The stabilizing moment about A of the wall for a partial safety factor $\gamma \mathrm{f}=1.0$ is


Fig. 5.4 Loads and earth pressures acting on the wall

Table 5.1 The resisting moments

| load (KN) | Distance from A (m) | Moment about A(KN.m) |
| :--- | :---: | :---: |
| $\mathrm{W}_{\text {wall 1 }}=27$ | 1.317 | 35.559 |
| $\mathrm{~W}_{\text {wall 2 }}=4.5$ | 1.13 | 5.085 |
| $\mathrm{~W}_{\text {floor }}=32$ | 1.6 | 51.2 |
| $\mathrm{~W}_{\text {back fill }}=109.179$ | 2.33 | 254.78 |
| $\mathrm{~W}_{\text {surcharge }}=86.65$ | 2.33 | 202.19 |
| Total $=259.76$ |  | 548.81 |

Table 5.2 The overturning moments

| Horizontal load (kN) | Distance from A(m) | Moment about A (kN. m) |
| :--- | :---: | :---: |
| Active pressure $\mathrm{E}_{\mathrm{a} 1}=66$ | 2 | 132 |
| $\mathrm{E}_{\mathrm{a} 2}=46.2$ | 1.33 | 61.446 |
| Total $=112.20$ |  | 193.44 |

$30.26+(211.97 * 1.28)=301.85 \mathrm{KN} . \mathrm{m}$
The overturning moment for a partial safety factor $\gamma \mathrm{f}=1.5$ is:

$$
\frac{M_{R}}{M_{0}}>1.5
$$

$\frac{548.81}{193.44}=2.8>1.5 \quad$ The wall is safe against overturning.
(iii) Resistance to sliding: The forces resisting sliding are the friction under the base and the passive resistance for the top of the base:

$$
\begin{aligned}
& \boldsymbol{F}_{S_{0}=\frac{\sum R_{V}}{\sum R_{H}} \boldsymbol{\mu}} \\
& \mu=\tan \emptyset=\tan 33=0.65
\end{aligned}
$$

$=\frac{259.76 * 0.65}{112.20}=1.5$
The resistance to sliding is satisfactory.
(iv) Over all comment the wall section is satisfactory.

The maximum soil pressure under the base controls the design.

## Structural design

### 5.3 Design retaining wall:

| Reference <br> Bs-8110- <br> 1997 | Calculation | Out put |
| :---: | :---: | :---: |
|  | The structural design is made for ultimate loads. The partial safety factor for each pressure and surcharge is $\gamma \mathrm{f}=1.4$. <br> The pressure at the top of the wall is $\begin{aligned} & \partial_{1}=1.4 \times 16.50=23.10 \mathrm{kN} / \mathrm{m}^{2} \\ & \partial_{2}=\mathrm{ka} *\left(\mathrm{q}+\mathrm{H}^{*} \gamma\right) \\ & =0.333 *(50+17.6 * 3.60)=39.73 \\ & \partial_{2}-\partial_{1}=39.73-23.10=16.63 \\ & 16.63 * 1.4=23.30 \\ & \text { Shear }=(23.10 \times 3.6)+(0.5 \times 3.6 \times 23.30) \\ & \quad=83.16+41.94=125.10 \mathrm{KN} \end{aligned}$ $\begin{aligned} \text { Moment } & =(83.16 \times 0.5 \times 3.6)+\left(41.94 \times \frac{3.60}{3}\right) \\ & =200 \mathrm{KN.} \mathrm{~m} \end{aligned}$ <br> The cover is 50 mm ; assume 16 mm diameter bars. Then $\mathrm{d}=400-50-8=342 \mathrm{~mm}$ $\begin{aligned} & \frac{\mathrm{M}}{\left(\mathrm{~b} * \mathrm{~d}^{2}\right)}=\frac{200 * 10^{6}}{\left(1000 * 342^{2}\right)}=1.70 \\ & \frac{100 \mathrm{~A}_{\mathrm{s}}}{\mathrm{~b} * \mathrm{~d}}=0.40(\text { figure } 4: 13) \\ & 100 \mathrm{~A}_{\mathrm{s}} /(342 * 1000)=0.40 \\ & =0.40 * 342 * 1000 / 100 \\ & \text { As }=1368 \mathrm{~mm}^{2} / \mathrm{m} \end{aligned}$ | $\begin{aligned} & \phi 16 \mathrm{~mm} @ 140 \\ & \mathrm{C} / \mathrm{C} \\ & \quad \approx 1407 \mathrm{~mm}^{2} / \mathrm{m} \end{aligned}$ |

Continue

| $\begin{aligned} & \text { Reference } \\ & \text { Bs-8110- } \\ & 1997 \end{aligned}$ | Calculation | Out put |
| :---: | :---: | :---: |
| clause <br> 3:4:5:2 <br> clause <br> 3.4.5.6 | The depth y 1 from the top where the 16 mm diameter bars can be reduced to a diameter of 12 mm . <br> As $=807 \mathrm{~mm}^{2}$ $=100 \times 807 /(1000 \times 342)=0.23$ $\frac{\mathrm{M}}{\mathrm{~b} * d^{2}}=1.25$ $\mathrm{M}=\frac{1.25 * 1000 * 342^{2}}{10^{6}}=146.205 \mathrm{KN} . \mathrm{m}$ $\mathrm{Mu}=\mathrm{M} * 1.4=1.4 * 146.205=204.687 \mathrm{kN} . \mathrm{m}$ <br> The depth y 1 is given by the equation $204.687=\frac{23.1 y_{1}{ }^{2}}{2}+\frac{1.4 * 5.87 y^{3}{ }_{1}}{6}$ <br> Or $\mathrm{y}_{1}{ }^{3}+8.43 \mathrm{y}_{1}{ }^{2}-149.5=0$ <br> Solve to give $y_{1}=3.53 \mathrm{~m}$. <br> The shear stress at the base of the wall is $\mathrm{V}=\frac{v}{\mathrm{~b} * \mathrm{~d}}=\frac{125.1 * 1000}{1000 * 342}=0.36 \mathrm{~N} / \mathrm{mm}^{2}$ <br> The design shear stress is $\begin{aligned} & \mathrm{V}_{C}=\frac{0.79\left(\frac{100 A_{\mathrm{s}}}{\mathrm{~b} * \mathrm{~d}}\right)^{\frac{1}{3}}\left(\frac{400}{342}\right)^{\frac{1}{4}}\left(\frac{\mathrm{Fcu}}{25}\right)^{\frac{1}{3}}}{1.25} \\ & \mathrm{~V}_{\mathrm{c}}=0.673 \mathrm{~N} / \mathrm{mm}^{2} \end{aligned}$ <br> The shear stress is satisfactory |  |

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| Reference Bs-8110- $1997$ | Calculation | Out put |
| :---: | :---: | :---: |
| clause 3:4:4:4 | For control of cracking the bar spacing must not exceed 3 times the effective depth. The spacing at the bars in the wall is 140 mm . <br> This is less than the 160 mm clear spacing given in Table 3.30 of the code for crack control. <br> For distribution steel provide the minimum area of $0.13 \%$ from Table 3.27 of the code $\mathrm{A}=0.0013 \times 1000 \times 400=520 \mathrm{~mm}^{2} / \mathrm{m}$ <br> Wall reinforcement (outer side) the pressure at the base of the wall is the pressure at the top of the wall is $\begin{aligned} & \mathrm{Pw}=\gamma_{\mathrm{w}} * \mathrm{H}=10 * 3.60=36.00 \mathrm{kN} / \mathrm{m}^{2} \\ & \mathrm{Pw}=1.4 * 36=50.40 \\ & \text { Shear }=0.5 \times 3.6 \times 50.40=90.72 \mathrm{kN} \\ & \text { Moment }=(90.72 \times 3.6 / 3)=108.86 \mathrm{kN} . \mathrm{M} \\ & \frac{\mathrm{M}}{\mathrm{~b} * d^{2}}=\frac{108.86 * 10^{6}}{1000 * 342^{2}}=0.93 \\ & \frac{100 \mathrm{~A}_{\mathrm{s}}}{1000 * 342}=0.4 \\ & \frac{0.4 * 342 * 1000}{100} \\ & \text { As }=1368 \mathrm{~mm}^{2} / \mathrm{m} \end{aligned}$ | \$ 12 @ 200 mm <br> C/C $\approx 565 \mathrm{~mm}^{2} / \mathrm{m}$ <br> horizontally on the outer face <br> \$ 16 mm @ 140 <br> C/C $\approx 1407 \mathrm{~mm}^{2} / \mathrm{m}$ |

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| $\begin{gathered} \text { Reference } \\ \text { Bs-8110-1997 } \end{gathered}$ | Calculation | Out put |
| :---: | :---: | :---: |
|  | iii) Inner footing Referring to Fig. 5.4 the shear and moment at the face of the wall are as follows: $\begin{aligned} & \text { Shear }=1.4 *\{(139.21 * 1.07)+(3.02 * 1.07 / 2) \\ & (32 * 1.07 / 3.20)\} \\ & =1.4(148.95+1.6-10.7)=195.79 \mathrm{KN} \end{aligned}$ <br> Moment $=1.4 *[(148.95-10.7) * 0.535$ $-(6 * 1.07 * 2 / 3)$ $=1.4(73.96-4.28)=97.55 \mathrm{kN} . \mathrm{m}$ $\frac{\mathrm{M}}{\mathrm{~b} * d^{2}}=\frac{97.55 * 10^{6}}{1000 * 342^{2}}=0834$ $\frac{100 \mathrm{~A}_{\mathrm{s}}}{\mathrm{~b} * \mathrm{~d}}=0.25$ $A_{S=\frac{0.25 * 1000 * 342}{}}^{100}=805 \mathrm{~mm}^{2} / \mathrm{m}$ <br> Shear stress $=\frac{195.79 * 10^{3}}{1000 * 342} \quad=0.57 \mathrm{~N} / \mathrm{mm}^{2}$ <br> This is satisfactory. <br> (iv) Outer footing Referring to Fig. 5.4 the shear and moment at the face of the wall are as follows: $\begin{aligned} & \text { Shear }=1.4^{*}\{(109.6+86.65)+(32 * 1.73) / 3.2- \\ & \left(8.25^{*} 1.73\right)_{-}\left(0.5 * 31.38^{*} 1.73\right\}= \\ & 1.4(109.6+86.65+17.3-14.72-17.143) \\ & =199.855 \mathrm{KN} \\ & \text { Moment }=1.4 *\{(0.865 * 198.83)- \\ & (17.143 * 0.4)\}=231.183 \mathrm{kN} . \mathrm{M} \end{aligned}$ | $\begin{aligned} & \phi 12 @ 125 \mathrm{~mm} \\ & \mathrm{C} / \mathrm{C} \\ & \approx 904 \mathrm{~mm}^{2} / \mathrm{m} \end{aligned}$ |

Continue

| Reference Bs-8110-1997 | Calculation | Out put |
| :---: | :---: | :---: |
|  | $\begin{aligned} & \frac{\mathrm{M}}{\mathrm{~b} * d^{2}}=\frac{231.18 * 10^{6}}{1000 * 342^{2}}=2.74 \\ & \frac{100 \mathrm{~A}_{\mathrm{s}}}{\mathrm{~b} * \mathrm{~d}}=0.55 \\ & A_{S=\frac{0.55 * 1000 * 342}{100}} \\ & =1881 \mathrm{~mm}^{2} / \mathrm{m} \end{aligned}$ $\text { Shear stress }=\frac{199.85 * 10^{3}}{1000 * 342}=0.58 \mathrm{~N} / \mathrm{mm}^{2}$ <br> This is satisfactory. <br> Crack width $\begin{aligned} & \mathrm{a}_{\mathrm{c}}=\frac{E_{S}}{E_{C}}=\frac{200}{28}=7.14 \\ & a_{c e}=a_{c} * \frac{A_{s}}{b * d}=7.14 * \frac{1407}{1000 * 342}=0.029 \\ & \frac{a_{c} * A_{s}}{b * d}=\frac{0.029 * 1407}{1000 * 342}=0.00012 \\ & \frac{\mathrm{x}}{\mathrm{~d}}=0.33 \text { from fig B.3 } \\ & \mathrm{X}=0.33 * 342=112.86 \mathrm{~mm} \\ & \frac{I_{c}}{\mathrm{~b} * \mathrm{~d}^{3}}=0.05 \text { from fig B. } 4 \\ & \mathrm{I}_{\mathrm{c}}=0.05 * 1000 *(342)^{3}=2000 * 10^{6} \mathrm{~mm}^{4} \\ & \varepsilon_{\mathrm{S}}=\frac{\mathrm{a}_{\mathrm{c}} M}{E_{S} * \mathrm{I}_{s}} *(\mathrm{~d}-\mathrm{x}) \\ & \varepsilon_{\mathrm{S}}=\frac{7.14 * 204.68 * 10^{6}}{200 * 10^{3} * 2000 * 10^{6}} *(342-112.86) \\ & =0.00083 \end{aligned}$ | $\begin{aligned} & \phi 16 @ 100 \\ & \mathrm{~mm} \mathrm{C/C} \\ & \approx 2010 \mathrm{~mm} \\ & / \mathrm{m} \end{aligned}$ |

Continue

| Reference <br> Bs-8110- <br> 1997 | Calculation | Out put |
| :--- | :--- | :--- |
|  | $\varepsilon_{h}=\frac{400-112.86}{342-112.86} * 0.00083=0.001$ |  |
| $\varepsilon_{m}=\varepsilon_{h}-\frac{b *(h-x)(a-x)}{3 E_{S} A_{S}(d-x)}=0.0004$ |  |  |
| Appendix B |  |  |
| eq.1 |  |  | | Design surface crack width $=$ <br> $1+2\left(\frac{\left.3 a_{c r} \varepsilon_{m}-c_{\text {min }}\right)}{h-x}\right)$ |  |
| :--- | :--- |
| $=$ | $3 * 76.5 * 0.0004$ <br> $1+2\left(\frac{76.5-50}{400-342}\right)$ <br> $0.081<0.2 \mathrm{~mm} \quad$ ok |



Fig. 5.5 Cross section of wall reinforcement

### 5.4 Design slab:



Continue

| $\begin{array}{\|c} \hline \text { Reference } \\ \text { Bs-8110- } \\ 1997 \end{array}$ | Calculation | Out put |
| :---: | :---: | :---: |
| clause <br> 3:4:5:2 <br> clause <br> 3.4.5.6 <br> equation 8 <br> equation 7 | Shear resistance $\begin{aligned} & \mathrm{V}=\frac{\mathrm{W}}{2}=\frac{10.55}{2}=5.27 \mathrm{KN} \\ & V=\frac{V}{b * d}=\frac{5.27 * 10^{3}}{1000 * 120}=0.44 \mathrm{~N} / \mathrm{mm}^{2} \\ & V_{c}=0.79\left(\frac{100 \mathrm{~A}_{\mathrm{S}}}{\mathrm{~b} * \mathrm{~d}}\right)^{\frac{1}{3}}\left(\frac{400}{120}\right)^{\frac{1}{4}}\left(\frac{\mathrm{~F}_{\mathrm{cu}}}{25}\right)^{\frac{1}{3}} / 1.25 \\ & =0.567>\mathrm{V} \quad \text { OK } \end{aligned}$ <br> Deflection <br> Actual $=$ span/effective depth $\begin{aligned} & =3200 / 120=26.67 \mathrm{~mm} \\ & \frac{\mathrm{M}}{\mathrm{~d} * b}=\frac{13.50 * 10^{6}}{1000 * 120}=0.93 \\ & \mathrm{~F}_{\mathrm{S}}=\frac{5}{8}\left(\frac{\mathrm{~F}_{\mathrm{Y}} A_{\text {req }}}{\mathrm{A}_{\mathrm{S} \text { Prov }}}\right)=\frac{5}{8}\left(\frac{460 * 296}{301}\right)=282.72 \mathrm{~N} / \mathrm{mm}^{2} \end{aligned}$ <br> The modification factor is $=0.55+\left(\frac{477-F_{S}}{120}\right)\left(0.9+\frac{M}{b d^{2}}\right)=1.4$ <br> allowable span $/ \mathrm{d}$ ratio $=1.4 * 20=28 \mathrm{~mm}$ <br> Actual $=$ span/effective depth $=26.67 \mathrm{~mm}$ <br> The slab is satisfactory with respect to deflection. |  |



Fig. 5.6 Cross section slab reinforcement

